

# Seismic Instruments

- The seismometer as a forced oscillator
  - The seismometer equation
  - Transfer function, resonance
  - Broadband sensors, accelerometers
  - Dynamic range and generator constant
- Rotation sensors
- Strainmeters
- Tiltmeters
- Global Positioning System (GPS)
- Ocean Bottom Seismometers (OBS)

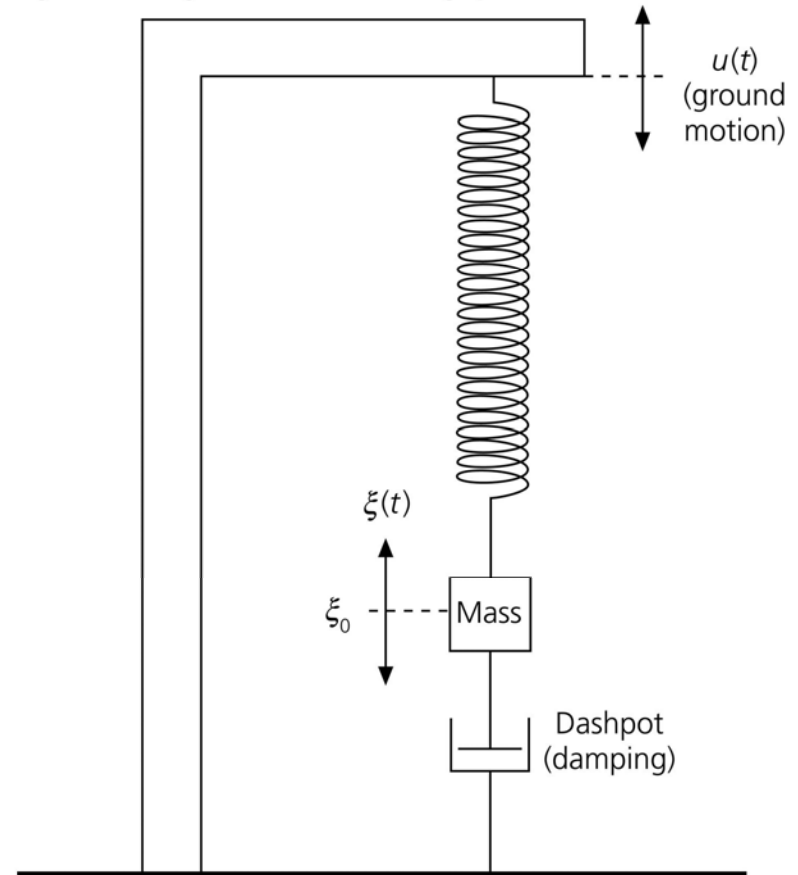
*Data examples, measurement principles, interconnections, accuracy, domains of application*

# Spring-mass seismometer

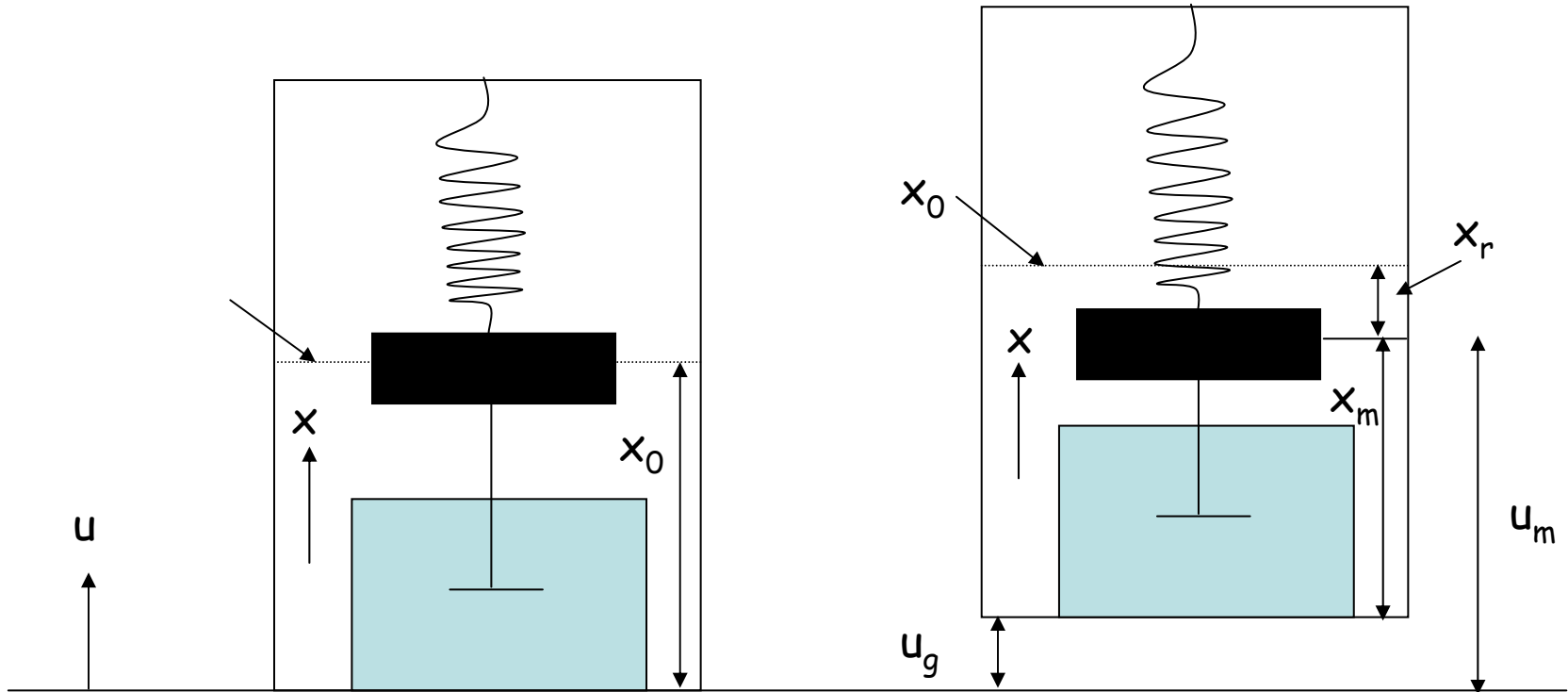
## vertical motion

Before we look more carefully at seismic instruments we ask ourselves what to expect for a typical spring based seismic inertial sensor. This will highlight several fundamental issues we have to deal with concerning seismic data analysis.

Figure 6.6-1: Diagram of a vertical seismograph.



# Seismometer – The basic principles



$u$  ground displacement  
 $x_r$  displacement of seismometer mass  
 $x_0$  mass equilibrium position

# Seismometer – The basic principles

The motion of the seismometer mass as a function of the ground displacement is given through a differential equation resulting from the equilibrium of forces (in rest):

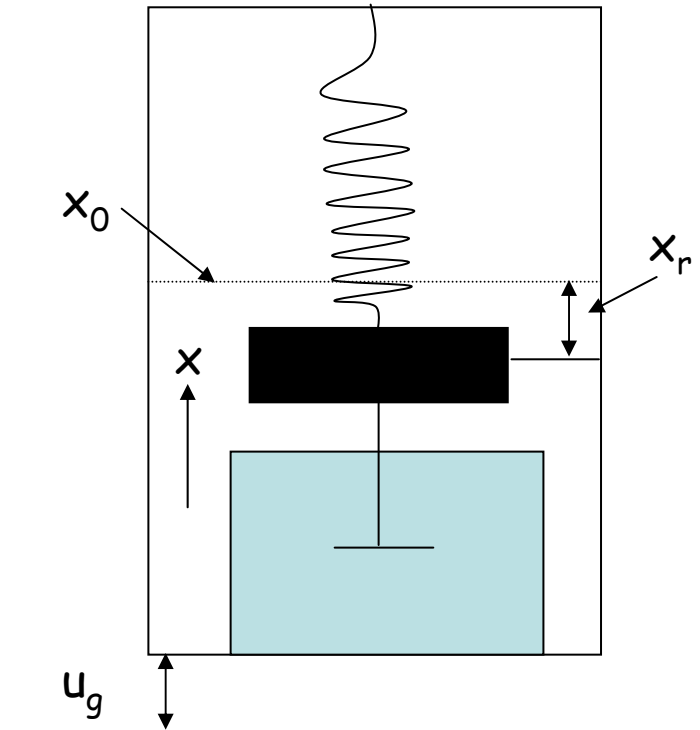
$$F_{\text{spring}} + F_{\text{friction}} + F_{\text{gravity}} = 0$$

for example

$$F_{\text{spring}} = -k x, k \text{ spring constant}$$

$$F_{\text{friction}} = -D \dot{x}, D \text{ friction coefficient}$$

$$F_{\text{gravity}} = -m\ddot{u}_g, m \text{ seismometer mass}$$



# Seismometer – The basic principles

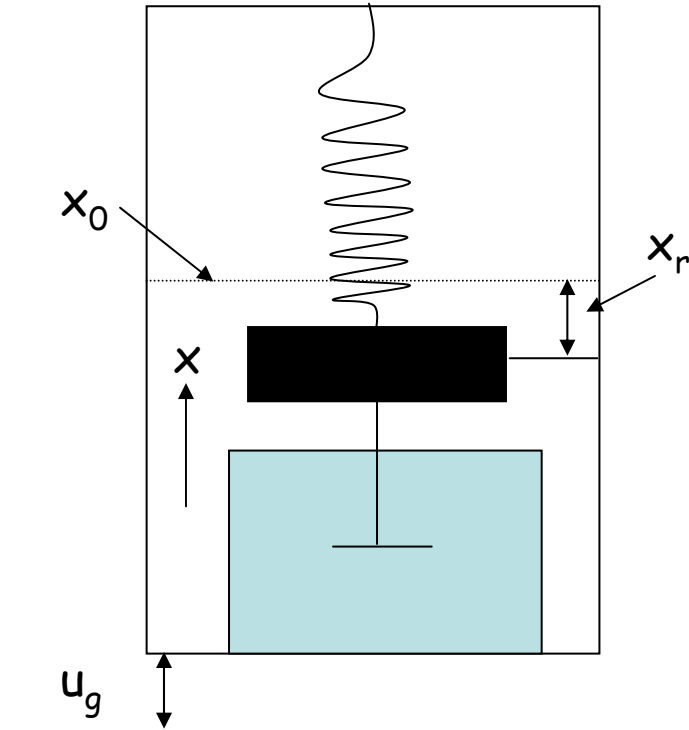
using the notation introduced above the equation of motion for the mass is

$$\ddot{x}_r(t) + 2\varepsilon\dot{x}_r(t) + \varpi_0^2 x_r(t) = -\ddot{u}_g(t)$$

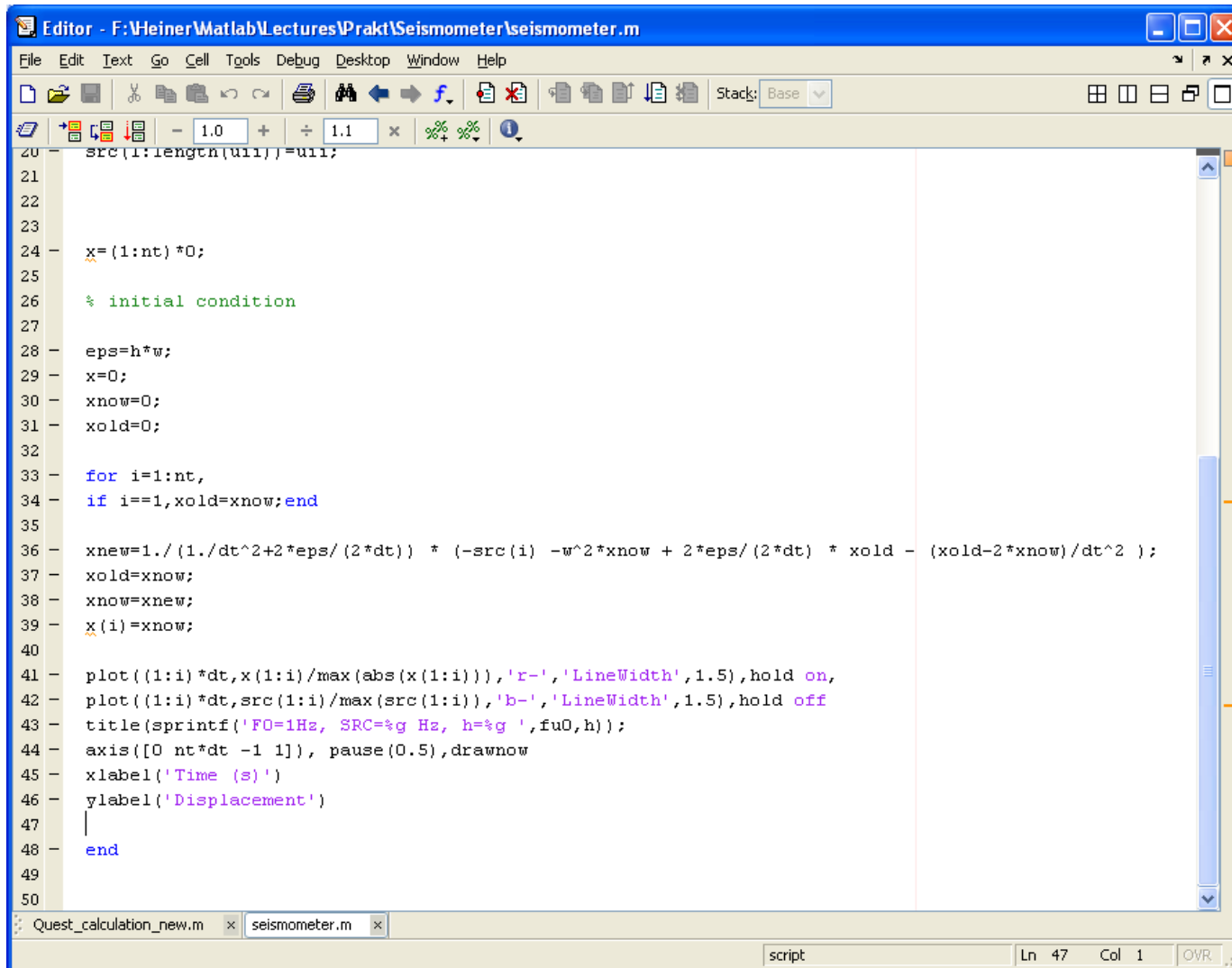
$$\varepsilon = \frac{D}{2m} = h\varpi_0, \quad \varpi_0^2 = \frac{k}{m}$$

From this we learn that:

- for slow movements the acceleration and velocity becomes negligible, the seismometer records ground acceleration
- for fast movements the acceleration of the mass dominates and the seismometer records ground displacement

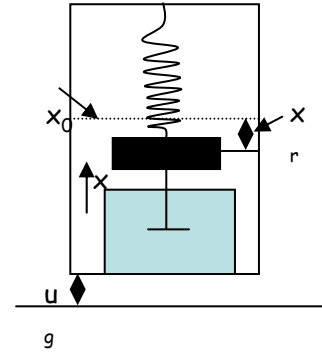
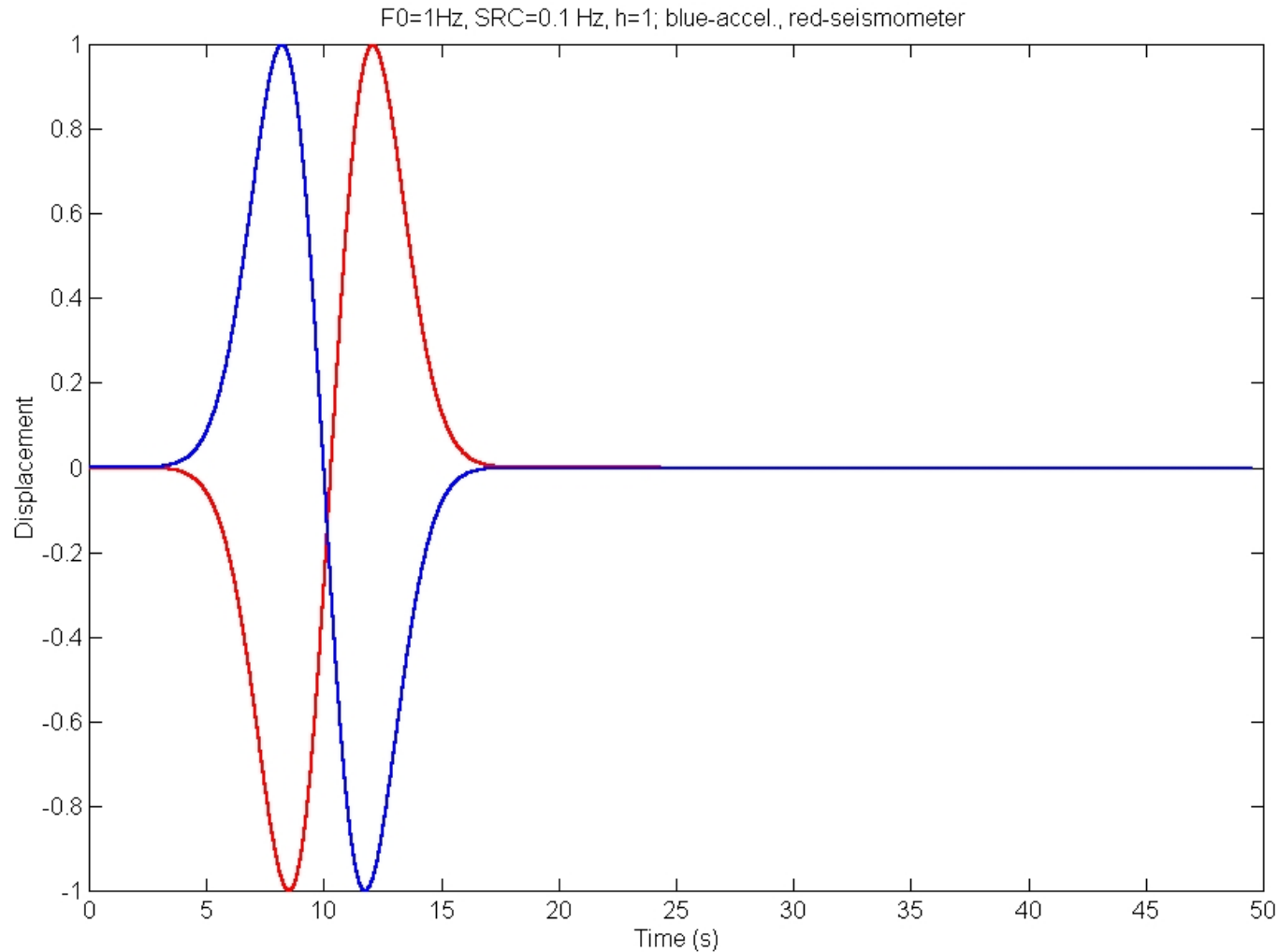


# A simple finite-difference solution of the seismometer equation

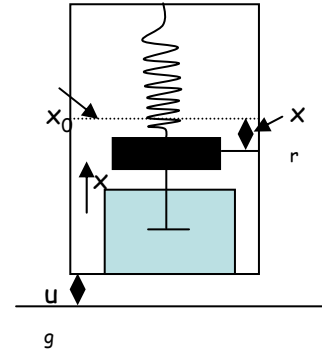
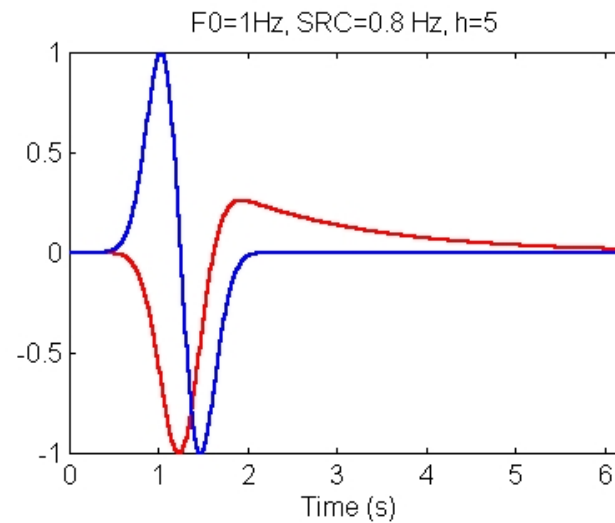
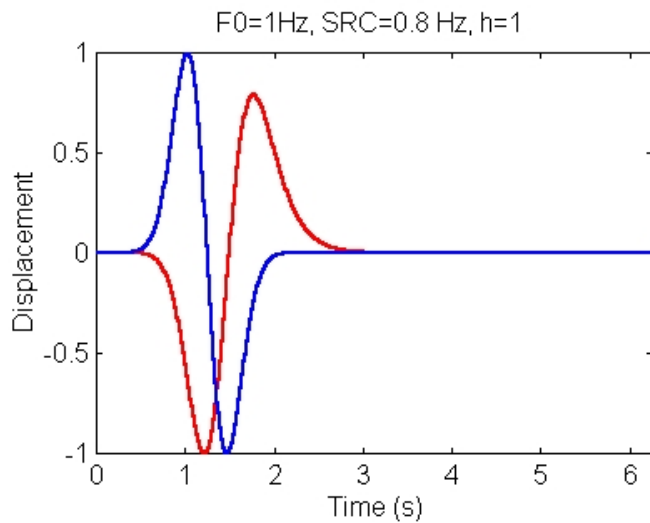
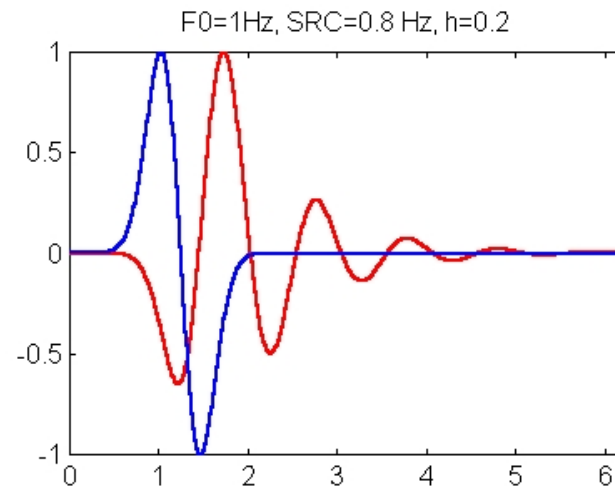
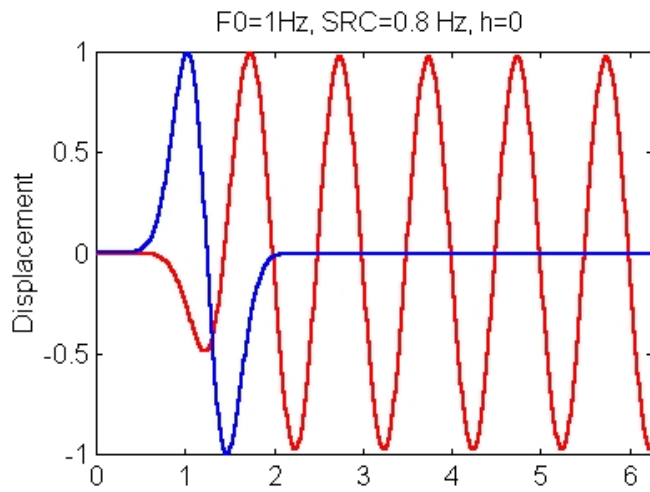


```
Editor - F:\Heiner\Matlab\Lectures\Prakt\Seismometer\seismometer.m
File Edit Text Go Cell Tools Debug Desktop Window Help
Stack: Base
- 1.0 + ÷ 1.1 × %>% %>%
20 - src(1:length(ui1))=ui1;
21
22
23
24 - x=(1:nt)*0;
25
26 % initial condition
27
28 - eps=h*w;
29 - x=0;
30 - xnow=0;
31 - xold=0;
32
33 - for i=1:nt,
34 - if i==1,xold=xnow;end
35
36 - xnew=1./(1./dt^2+2*eps/(2*dt)) * (-src(i) -w^2*xnow + 2*eps/(2*dt) * xold - (xold-2*xnow)/dt^2 );
37 - xold=xnow;
38 - xnow=xnew;
39 - x(i)=xnow;
40
41 - plot((1:i)*dt,x(1:i)/max(abs(x(1:i))), 'r-', 'LineWidth', 1.5), hold on,
42 - plot((1:i)*dt,src(1:i)/max(src(1:i)), 'b-', 'LineWidth', 1.5), hold off
43 - title(sprintf('FO=1Hz, SRC=%g Hz, h=%g ',fu0,h));
44 - axis([0 nt*dt -1 1]), pause(0.5),drawnow
45 - xlabel('Time (s)')
46 - ylabel('Displacement')
47 - |
48 - end
49
50
Quest_calculation_new.m x seismometer.m x
script Ln 47 Col 1 OVR
```

# Seismometer – examples



# Varying damping constant



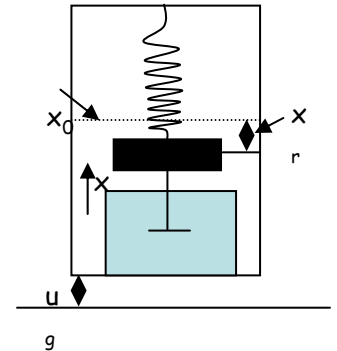


# Seismometer – Calibration

1. How can we determine the damping properties from the observed behaviour of the seismometer?

2. How does the seismometer amplify the ground motion? Is this amplification frequency dependent?

We need to answer these question in order to determine what we really want to know:  
The ground motion.

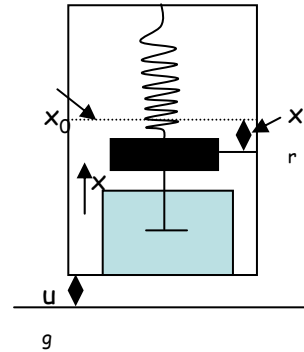


# Seismometer – Release Test

1. How can we determine the damping properties from the observed behaviour of the seismometer?

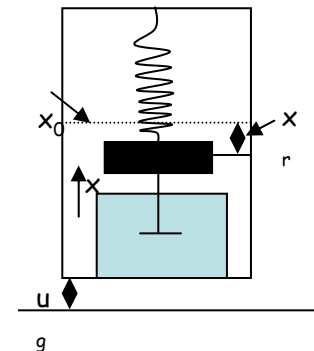
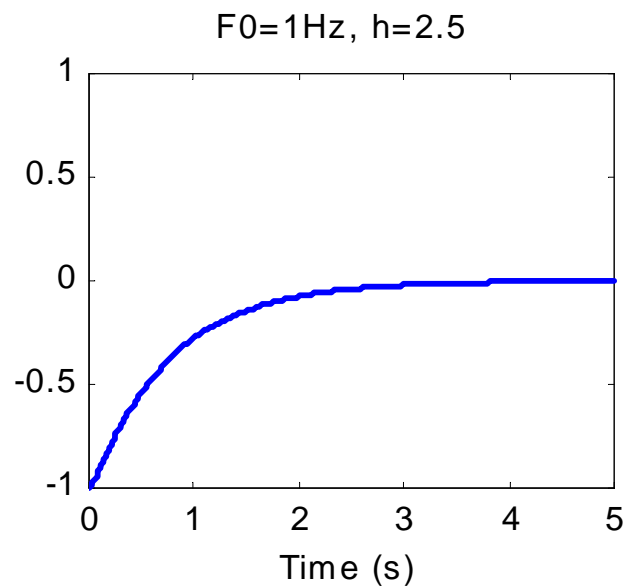
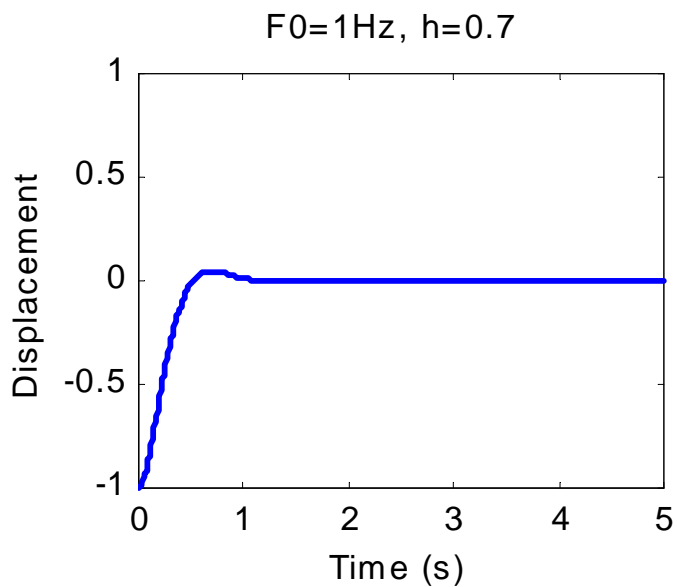
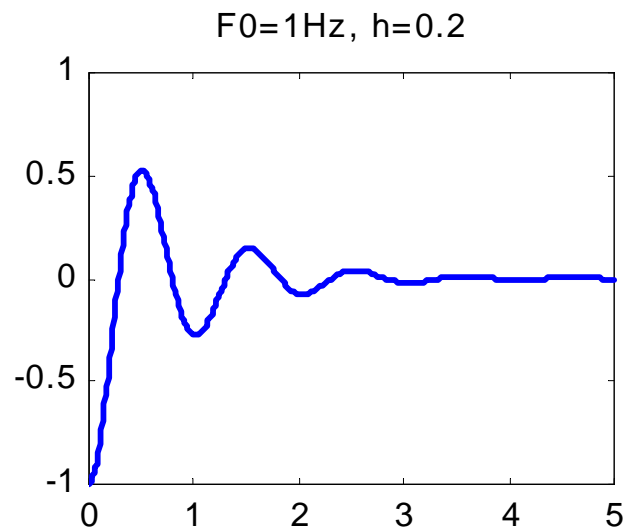
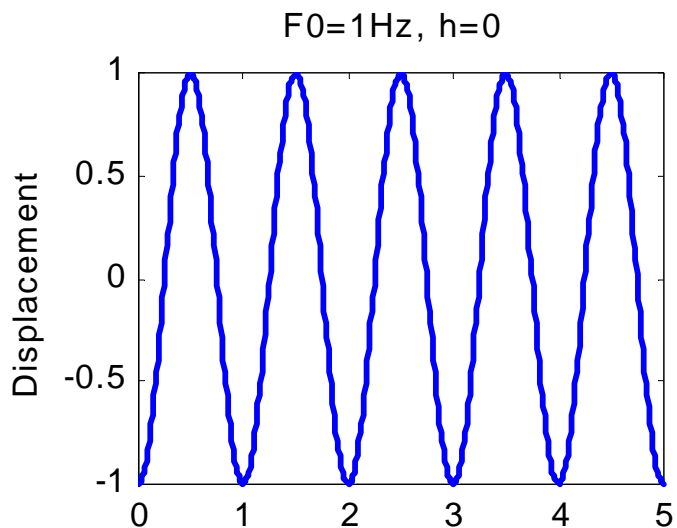
$$\ddot{x}_r(t) + h\omega_0\dot{x}_r(t) + \omega_0^2x_r(t) = 0$$
$$x_r(0) = x_0, \quad \dot{x}_r(0) = 0$$

We release the seismometer mass from a given initial position and let it swing. The behaviour depends on the relation between the frequency of the spring and the damping parameter. **If the seismometers oscillates, we can determine the damping coefficient  $h$ .**

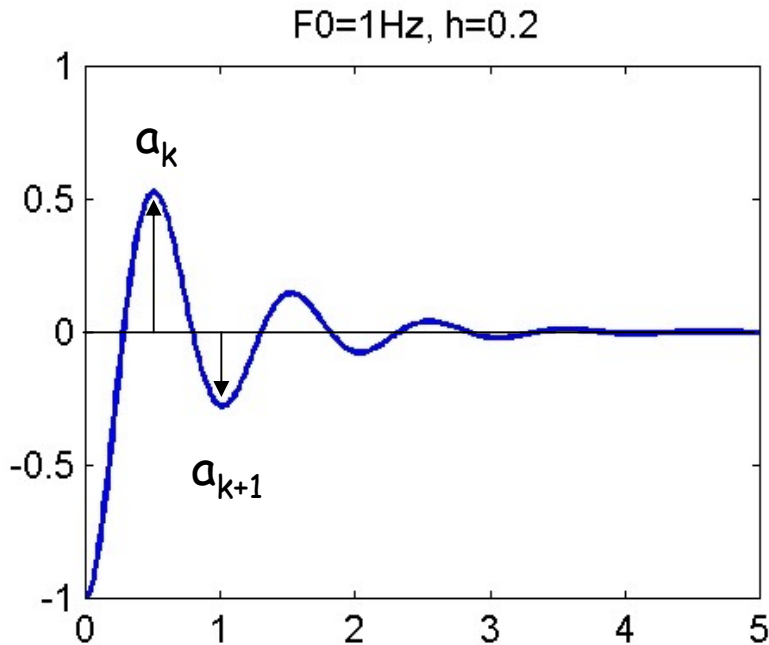


9

# Seismometer – Release Test



# Seismometer – Release Test

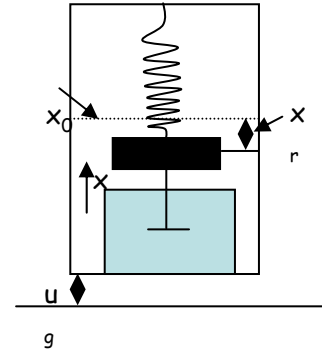


The damping coefficients can be determined from the amplitudes of consecutive extrema  $a_k$  and  $a_{k+1}$ . We need the logarithmic decrement  $\Lambda$

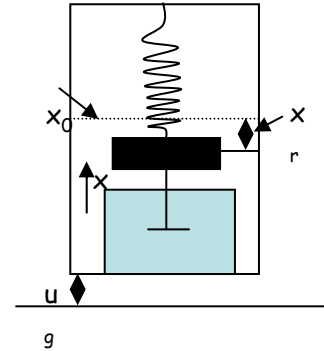
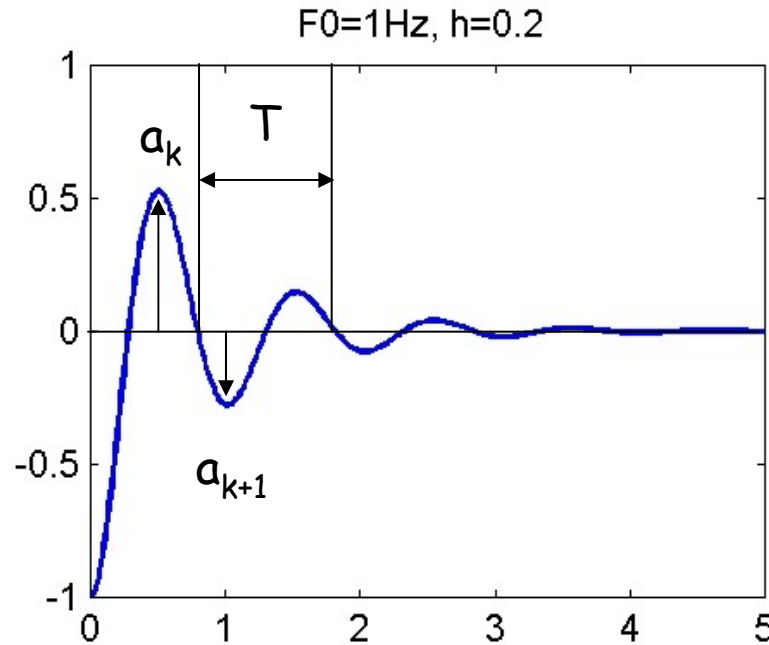
$$\Lambda = 2 \ln \left( \frac{a_k}{a_{k+1}} \right)$$

The damping constant  $h$  can then be determined through:

$$h = \frac{\Lambda}{\sqrt{4\pi^2 + \Lambda^2}}$$



# Seismometer – Frequency



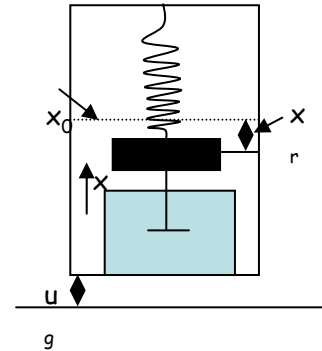
The period  $T$  with which the seismometer mass oscillates depends on  $h$  and (for  $h < 1$ ) is always larger than the period of the spring  $T_0$ :

$$T = \frac{T_0}{\sqrt{1-h^2}}$$

# Seismometer – Response Function

2. How does the seismometer amplify the ground motion? Is this amplification frequency dependent?

To answer this question we excite our seismometer with a monofrequent signal and record the response of the seismometer:

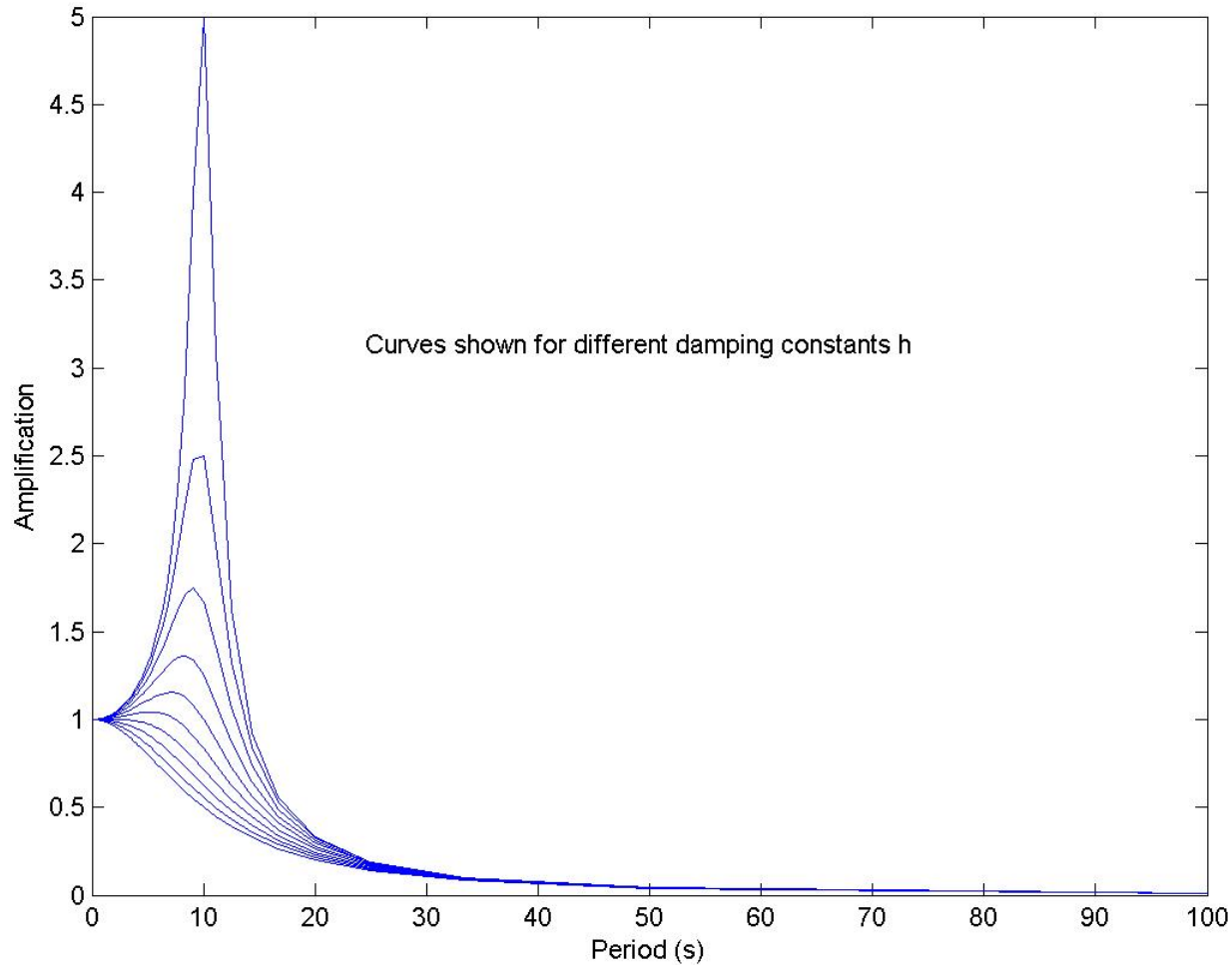


$$\ddot{x}_r(t) + h\omega_0\dot{x}_r(t) + \omega_0^2x_r(t) = \omega^2A_0e^{i\omega t}$$

the amplitude **response**  $A_r$  of the seismometer depends on the frequency of the seismometer  $\omega_0$ , the frequency of the excitation  $\omega$  and the damping constant  $h$ :

$$\left| \frac{A_r}{A_0} \right| = \frac{1}{\sqrt{\left( \frac{T^2}{T_0^2} - 1 \right)^2 + 4h^2 \frac{T^2}{T_0^2}}}$$

# Amplitude Response Function - Resonance

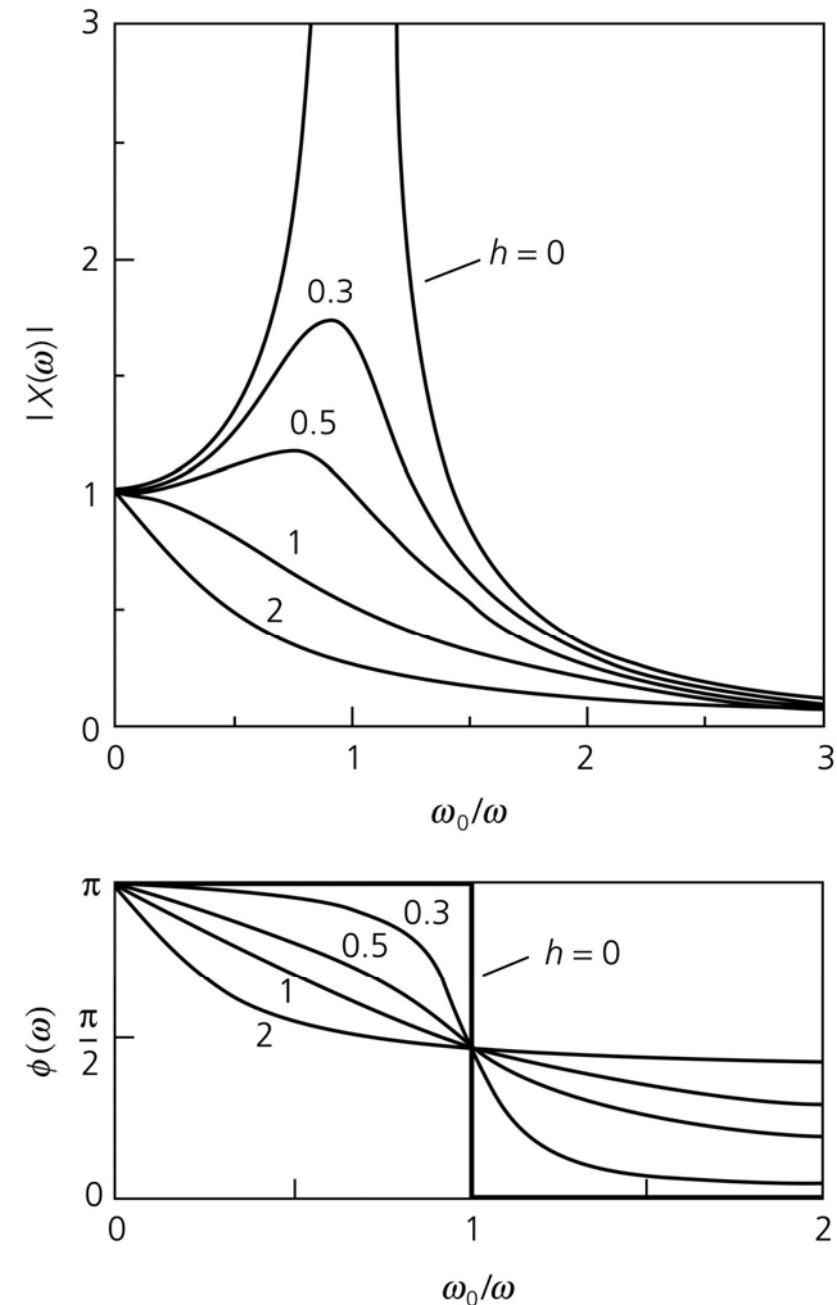


# Phase Response

Clearly, the amplitude and phase response of the seismometer mass leads to a severe distortion of the original input signal (i.e., ground motion).

Before analysing seismic signals this distortion has to be reversed:

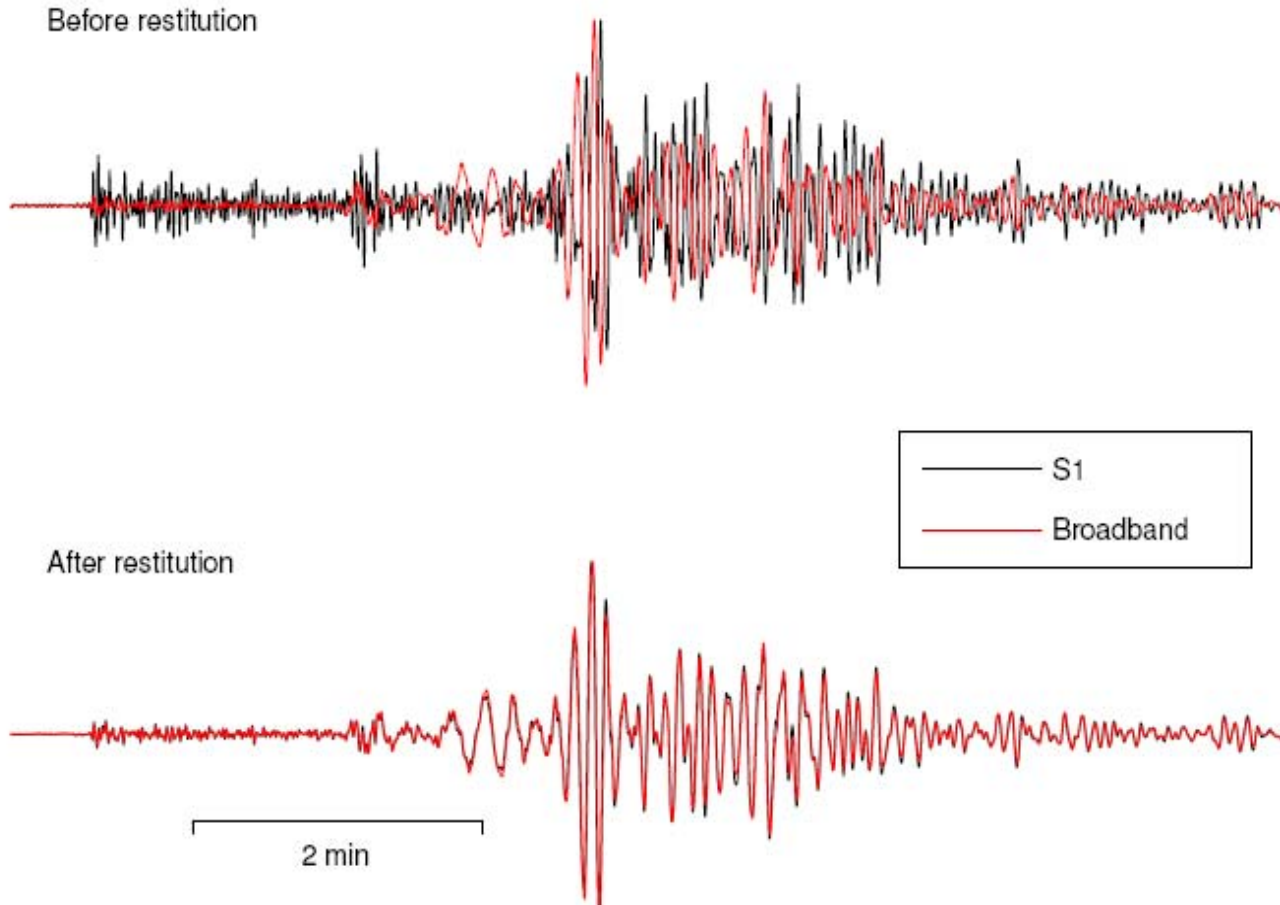
-> **Instrument correction**





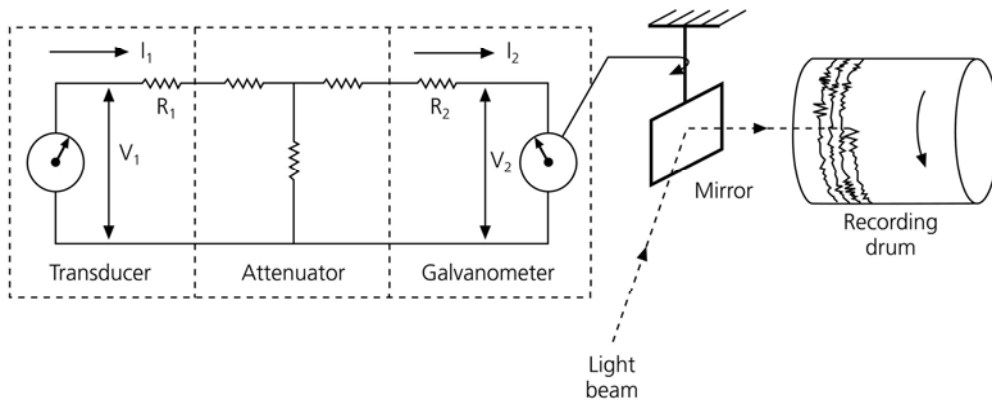
# Seismometer as a Filter

Restitution -> Instrument correction



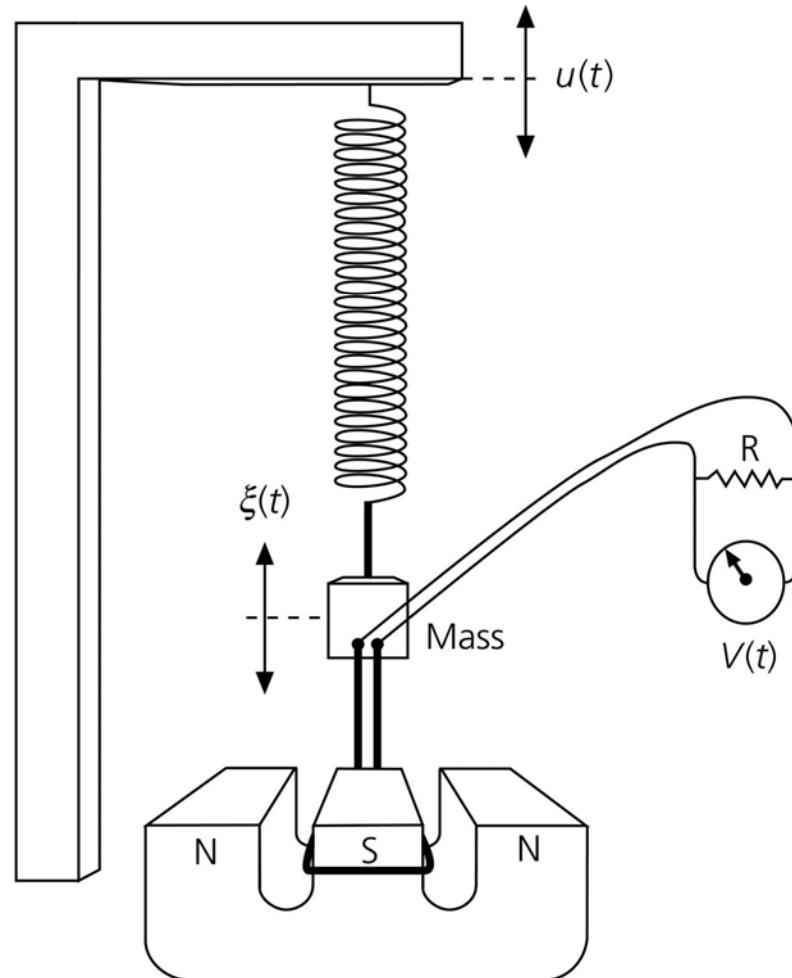
# Electromagnetic Seismograph

Figure 6.6-6: Coupling of the transducer of an electromagnetic seismograph to a galvanometer.



Electromagnetic seismographs measure **ground velocity**

Figure 6.6-5: Illustration of an electromagnetic seismograph.



# Seismic signal and noise

The observation of seismic noise had a strong impact on the design of seismic instruments, the separation into **short-period** and **long-period** instruments and eventually to the development of **broadband sensors**.

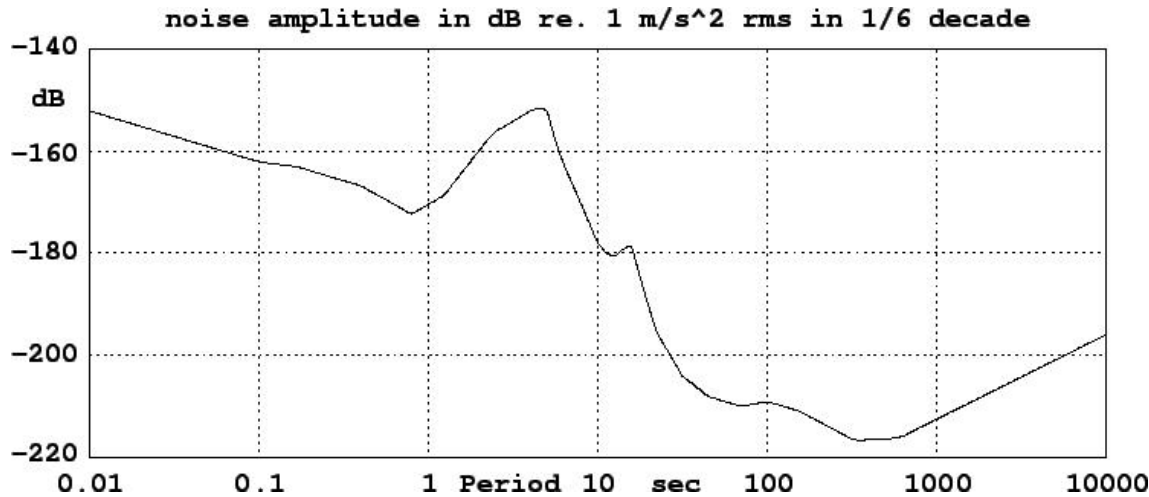
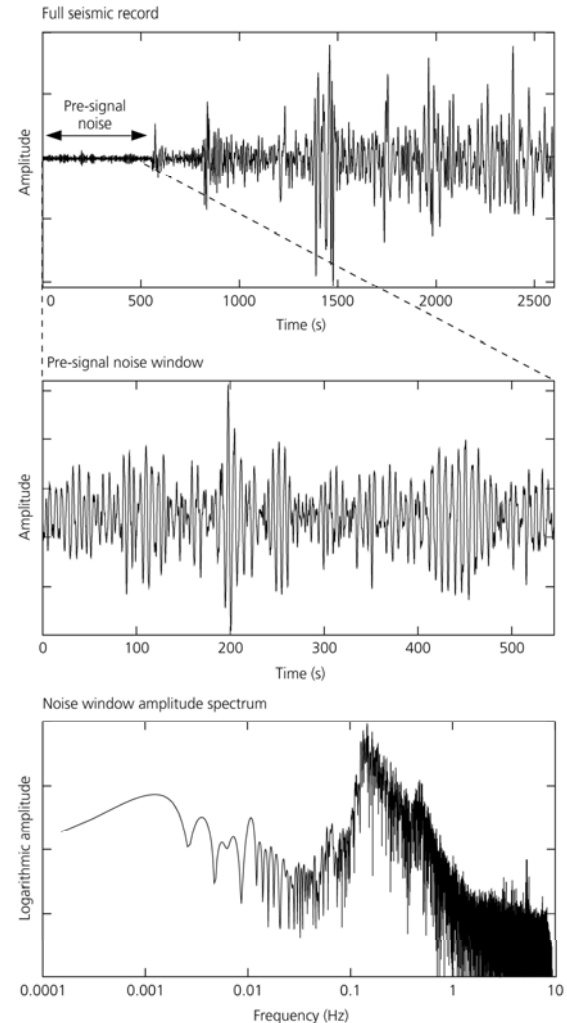
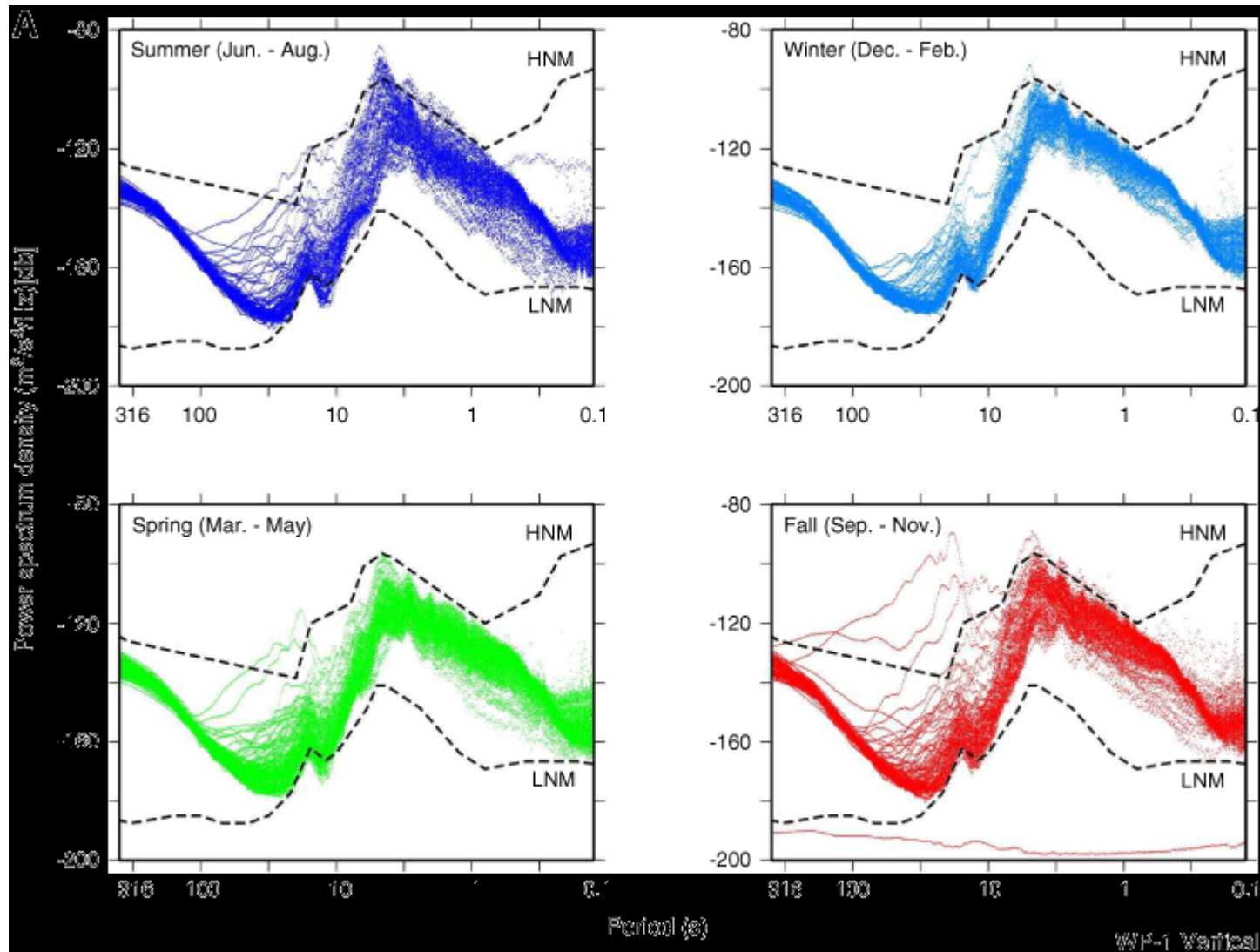


Figure 6.6-3: Demonstration of seismic noise on a broadband seismogram.

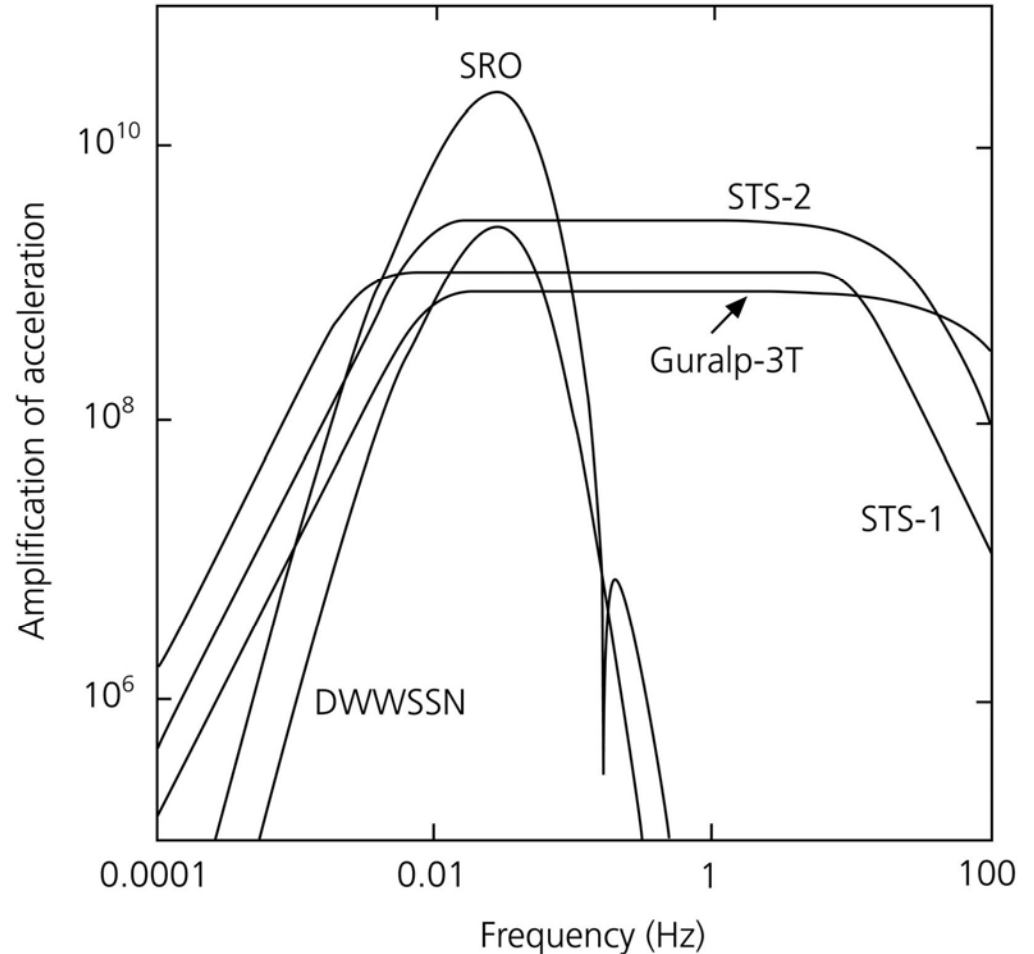


# Seismic noise



# Seismometer Bandwidth

Figure 6.6-8: Instrument responses for several types of seismometers.



Today most of the sensors of permanent and temporary seismic networks are broadband instruments such as the STS1+2.

Short period instruments are used for local seismic events (e.g., the Bavarian seismic network).

# The STS-2 Seismometer

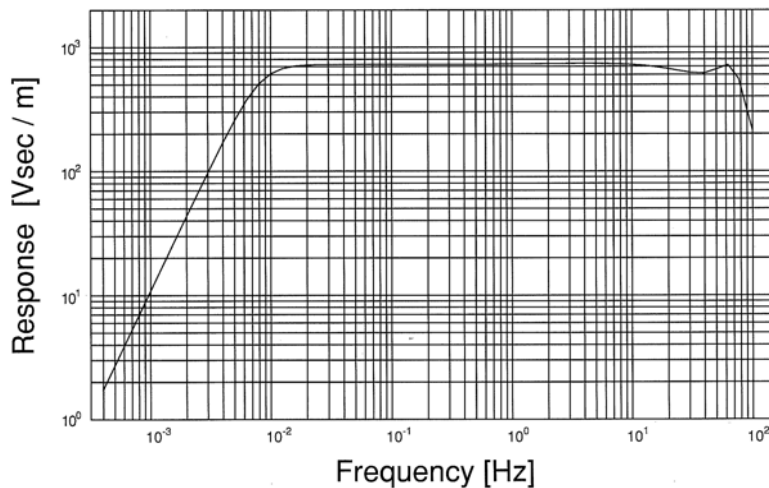
Environmental protection Vacuum-tight, low-stress construction

**Electro-mechanical**

Item	Standard Power	Low-Power
Generator constant		2 x 750 Vsec/m
Response	Ground velocity between corners 8.33 mHz (120 sec) and > 50 Hz.	
Seismic signal output	± 20 V differential range, 220 Ohms serial resistance per line	
Auxiliary outputs	± 10 V single-ended, 1 kilohm serial	
Electronic self-noise	typically 6 dB below USGS low-noise model between 5 mHz and > 10 Hz	typically 6 dB below USGS low-noise model between 5 mHz and 1 Hz, below USGS low-noise model between 1 Hz and 10 Hz
Clip level	± 13 mm/sec ground velocity up to 20 Hz, linear derating from 20 Hz to 50 Hz down to 5.3 mm/sec at 50 Hz	
Clip level normalized to gravity		
Dynamic range		
Parasitic resonances		



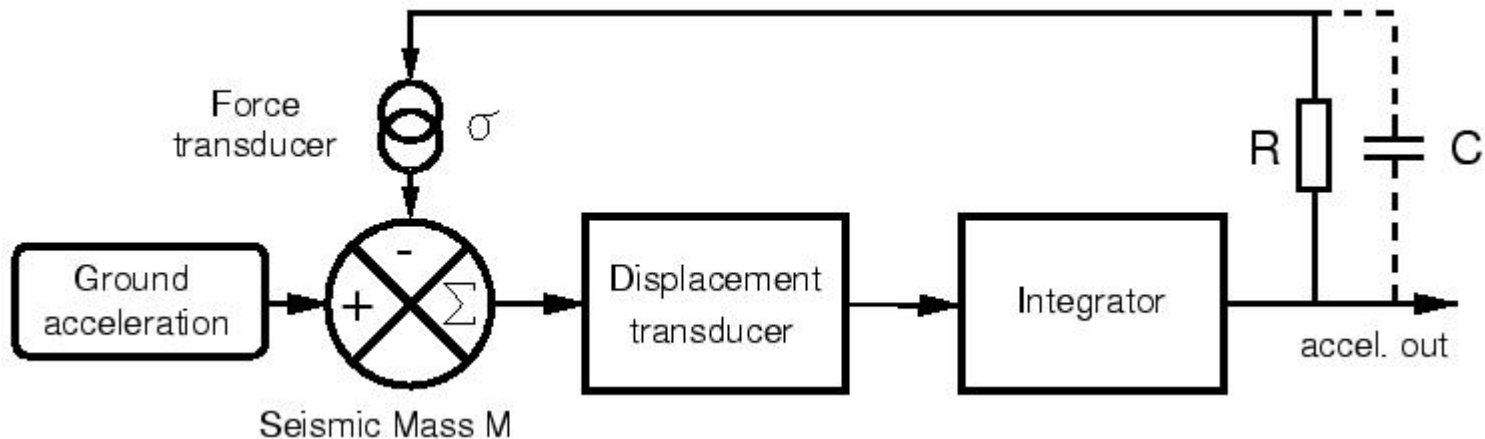
**STS-2 VELOCITY RESPONSE**



[www.kinematics.com](http://www.kinematics.com)

# Accelerometer

## force-balance principle



Feedback circuit of a force-balance accelerometer (FBA). The motion of the mass is controlled by the sum of two forces: the inertial force due to ground acceleration, and the negative feedback force. The electronic circuit adjusts the feedback force so that the two forces very nearly cancel. (Source Stuttgart University)

# Accelerometer

basalt.pdf [application/pdf Objekt] - Mozilla Firefox

http://www.kinometrics.com/pdf/basalt.pdf

Acquisition modes:	Continuous, triggered, time windows
Output data format:	24 bit signed (3 bytes) in user selectable for
Parameter calculations:	Calculations of key parameters in real-time
Real time digital output:	Ethernet or RS-232 output of digital stream (factory for available formats)

**Sensor**

Type:	Triaxial EpiSensor Force Balance Accelerometer, Orthogonally oriented, Internal or External
Full scale range:	User selectable at $\pm 0.25g$ , $\pm 0.5g$ , $\pm 1g$ , $\pm 2g$ or $\pm 4g$
Bandwidth:	DC to 200 Hz
Dynamic range:	155 dB+
Calibration & test:	Calibr. Coil Functional Test; Calibr.Coil Response Test

**Trigger**

Type:	IIR bandpass filter (three types available)
Trigger selection:	Independently selected for each channel
Threshold trigger:	Selectable from 0.01% to 100% of full scale



[www.kinometrics.com](http://www.kinometrics.com)



# (Relative) Dynamic range

What is the precision of the sampling of our physical signal in amplitude?

**Dynamic range:** the ratio between largest measurable amplitude  $A_{\max}$  to the smallest measurable amplitude  $A_{\min}$ .

The unit is Decibel (dB) and is defined as the ratio of two power values (and power is proportional to amplitude square)

In terms of amplitudes

$$\text{Dynamic range} = 20 \log_{10}(A_{\max}/A_{\min}) \text{ dB}$$

Example: with 1024 units of amplitude ( $A_{\min}=1$ ,  $A_{\max}=1024$ )

$$20 \log_{10}(1024/1) \text{ dB} \sim 60 \text{ dB}$$

# Dynamic range of a seismometer ADC (analog-digital-converter)

A n-bit digitizer will have  $2^{n-1}$  intervals to describe an analog signal.

Example:

A 24-bit digitizer has 5V maximum output signal (full-scale-voltage)

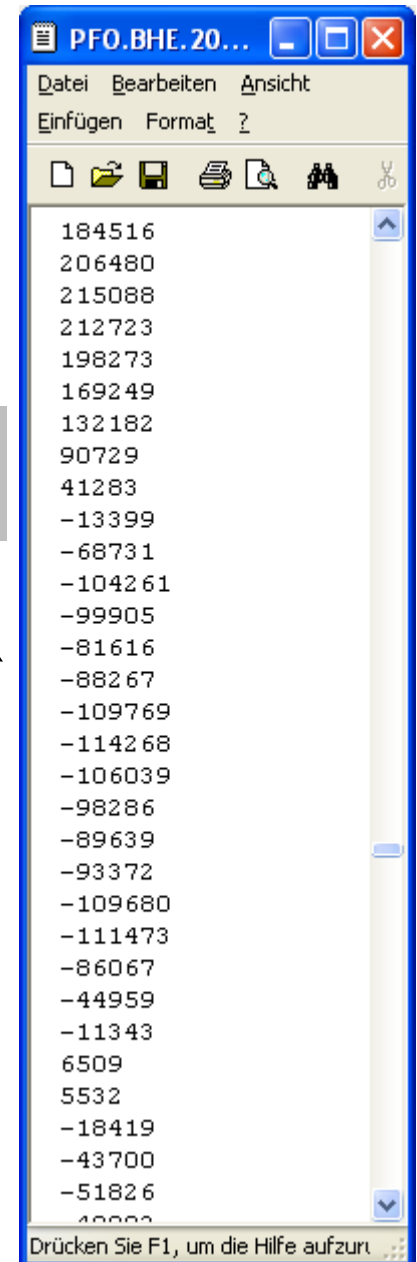
The least significant bit (lsb) is then

$$\text{lsb} = 5\text{V} / 2^{n-1} = 0.6 \text{ microV}$$

Generator constant STS-2: 750 Vs/m

What does this imply for the peak ground velocity at 5V?

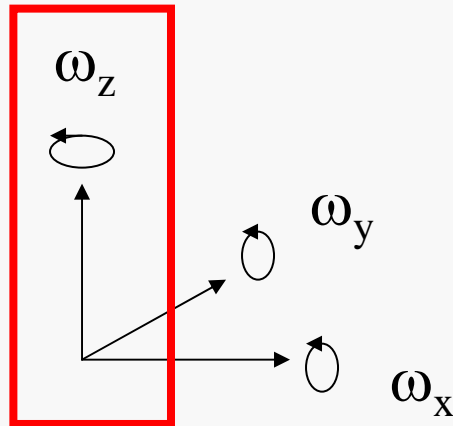
Seismogram data  
in counts



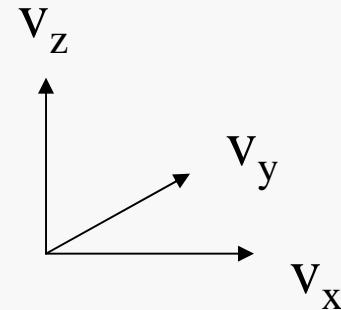
# Rotation

the **curl** of the wavefield

$$\begin{pmatrix} \omega_x \\ \omega_y \\ \omega_z \end{pmatrix} = \frac{1}{2} \nabla \times \underline{\mathbf{v}} = \frac{1}{2} \begin{pmatrix} \partial_y v_z - \partial_z v_y \\ \partial_z v_x - \partial_x v_z \\ \partial_x v_y - \partial_y v_x \end{pmatrix}$$

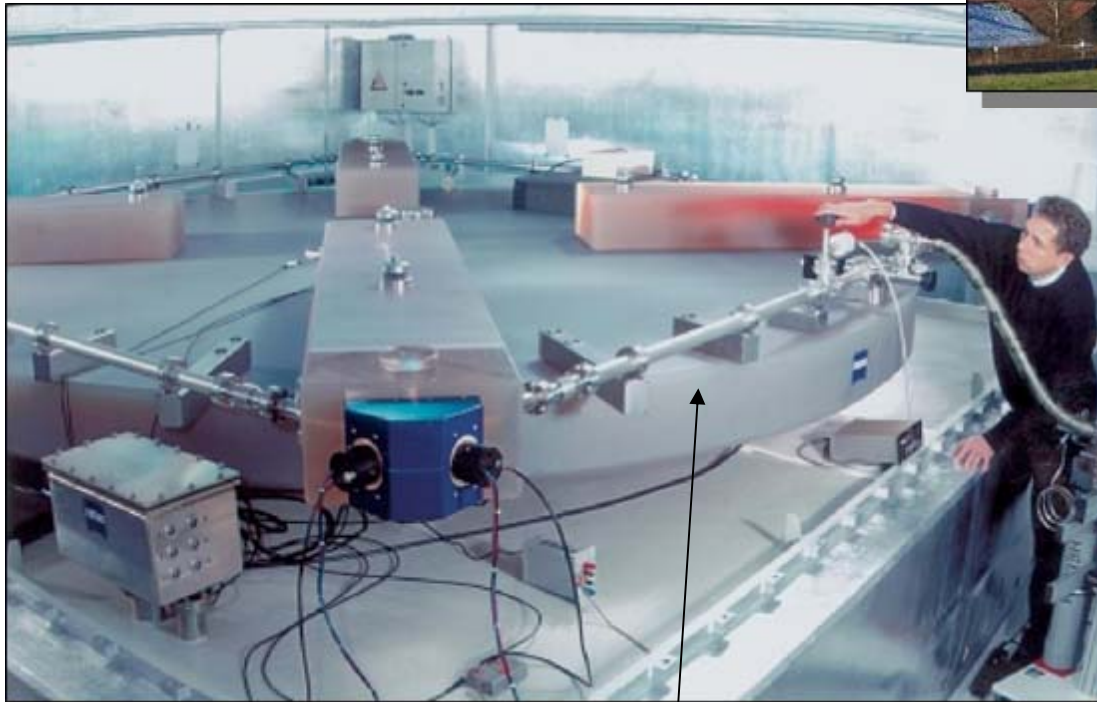


Rotation rate  
***Rotation sensor***



Ground velocity  
***Seismometer***

# The ring laser at Wettzell



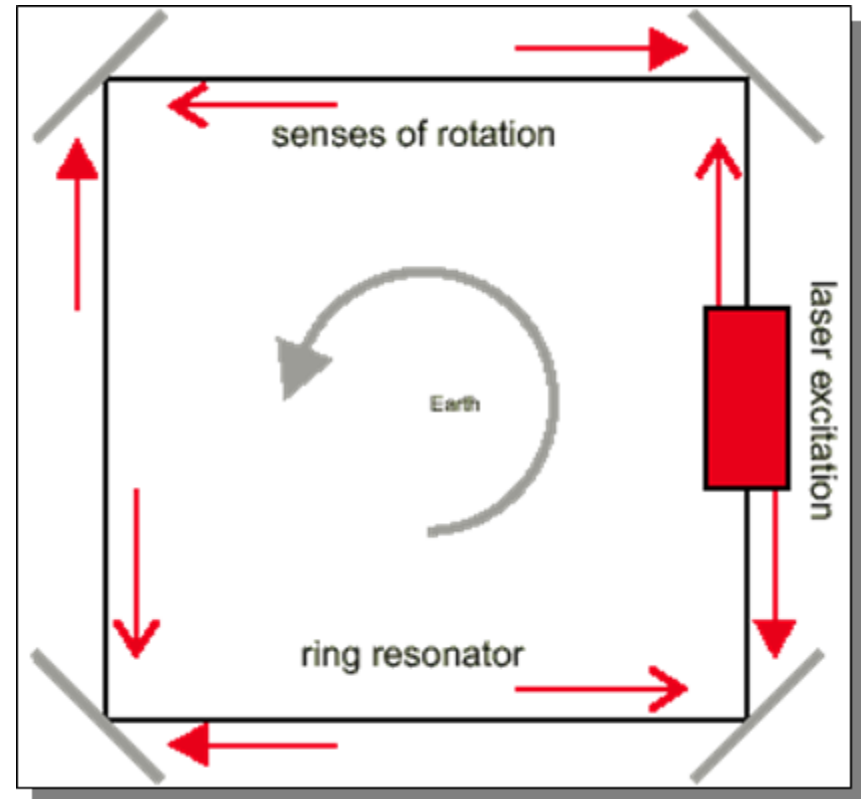
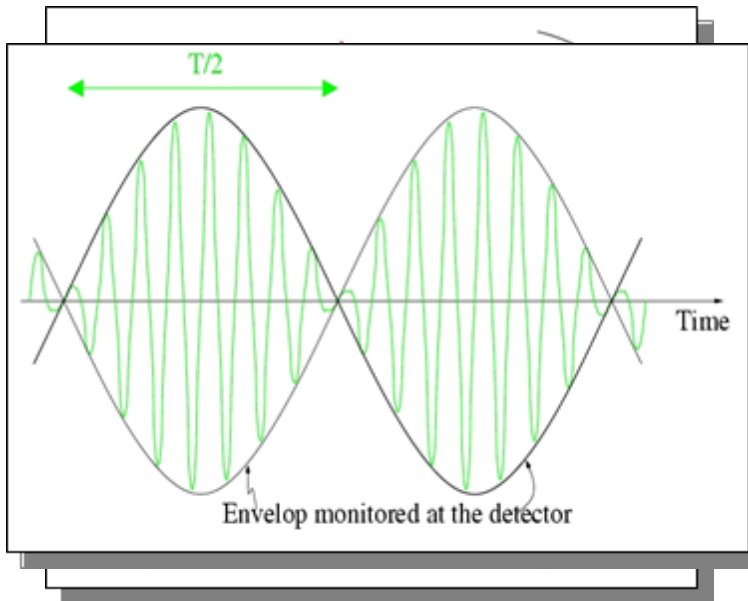
ring laser



Data accessible at [www.rotational-seismology.org](http://www.rotational-seismology.org)

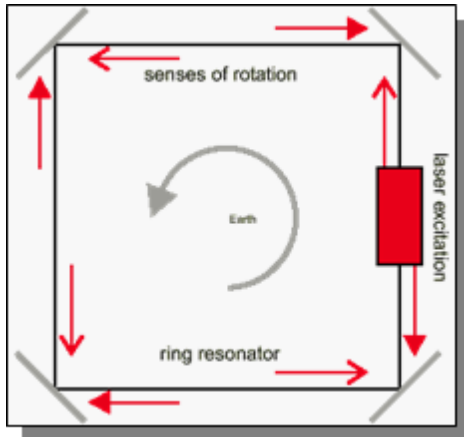
# How can we observe rotations?

-> ring laser



Ring laser technology developed by the groups at the Technical University Munich and the University of Christchurch, NZ

# Ring laser – the principle

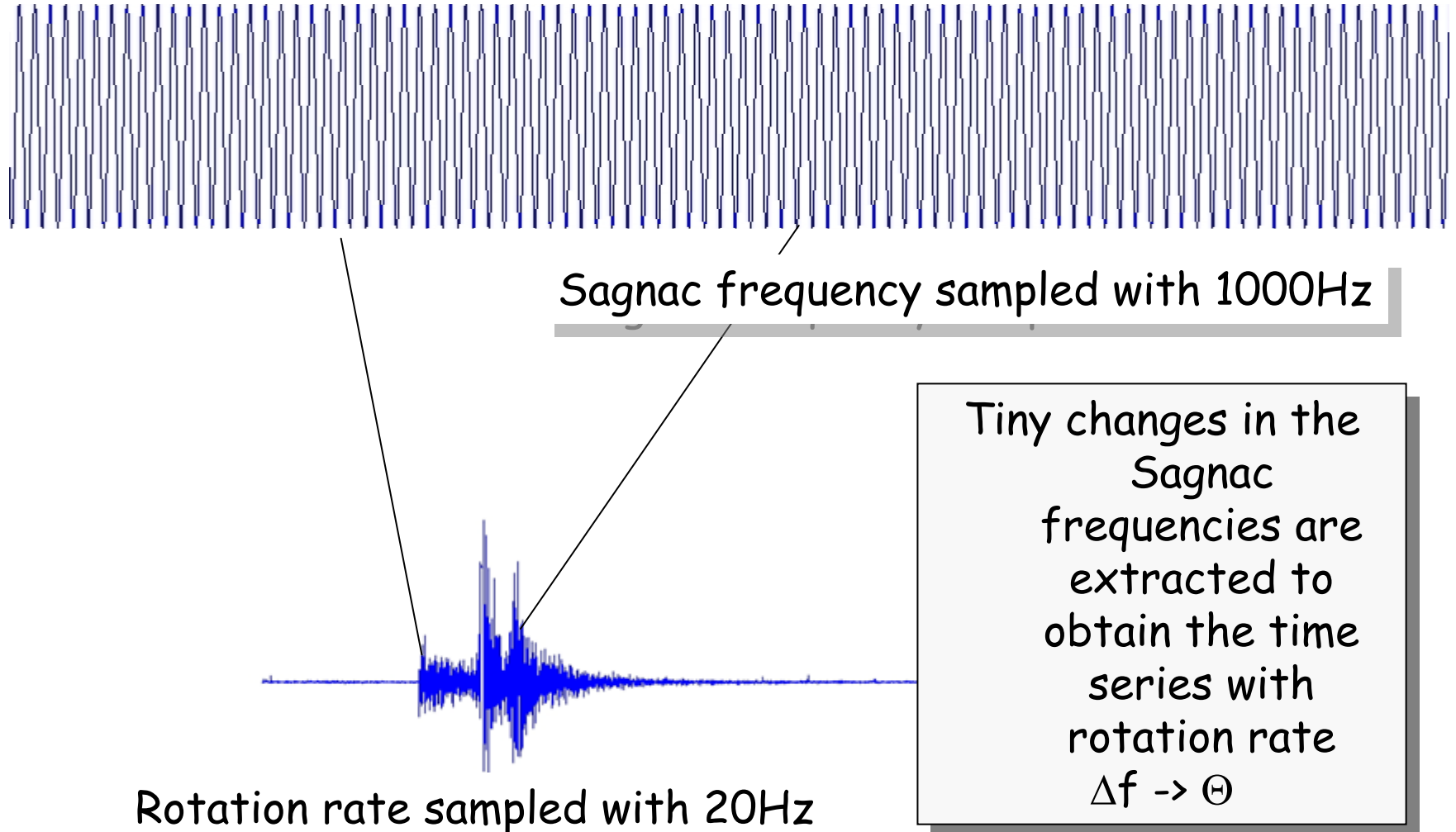


$$\Delta f_{Sagnac} = \frac{4\Omega \cdot A}{\lambda P}$$

- A surface of the ring laser (vector)
- $\Omega$  imposed rotation rate (Earth's rotation + earthquake +...)
- $\lambda$  laser wavelength (e.g. 633 nm)
- P perimeter (e.g. 4-16m)
- $\Delta f$  Sagnac frequency (e.g. 348,6 Hz sampled at 1000Hz)

# The Sagnac Frequency

(schematically)

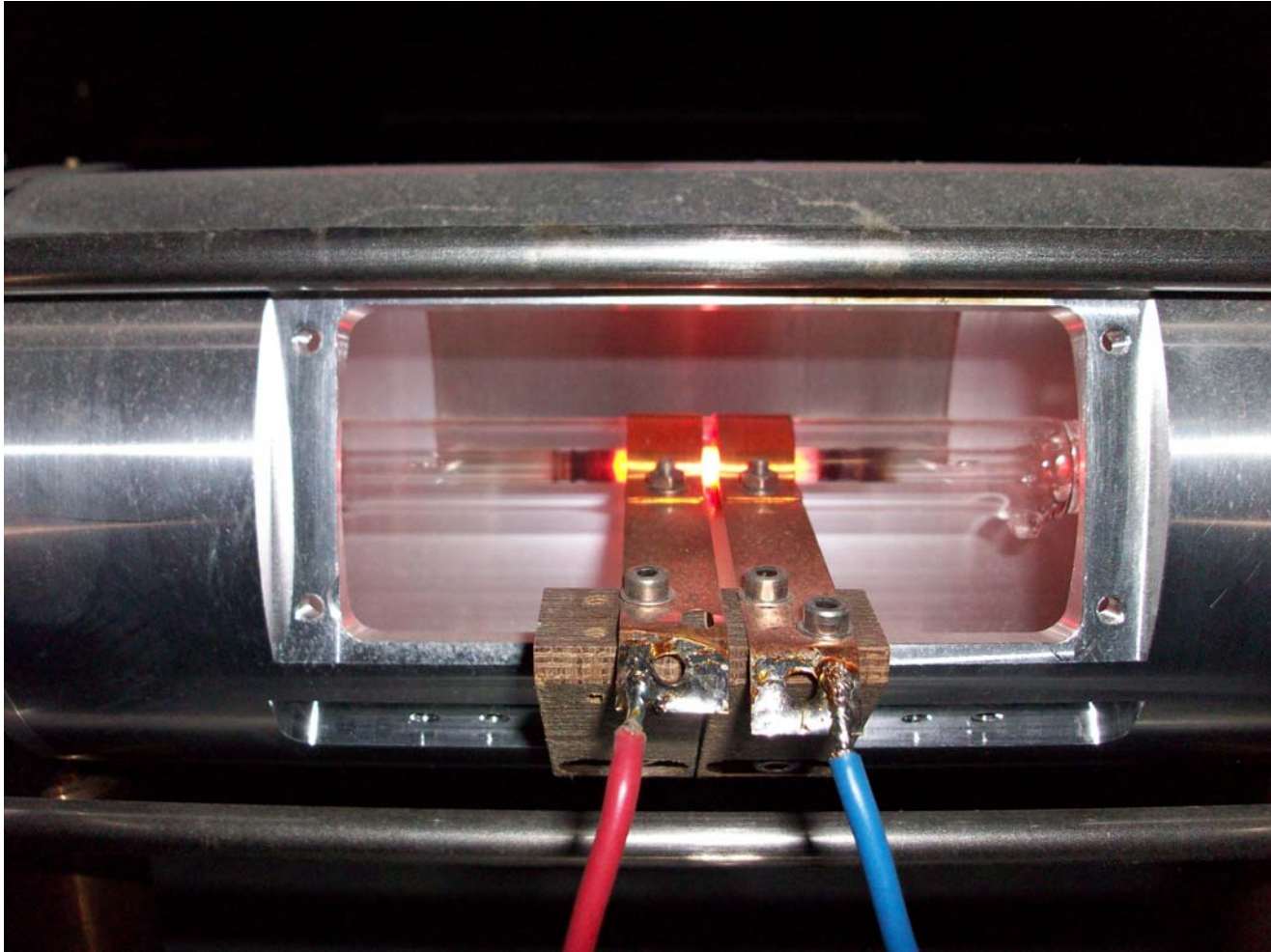


# The PFO sensor

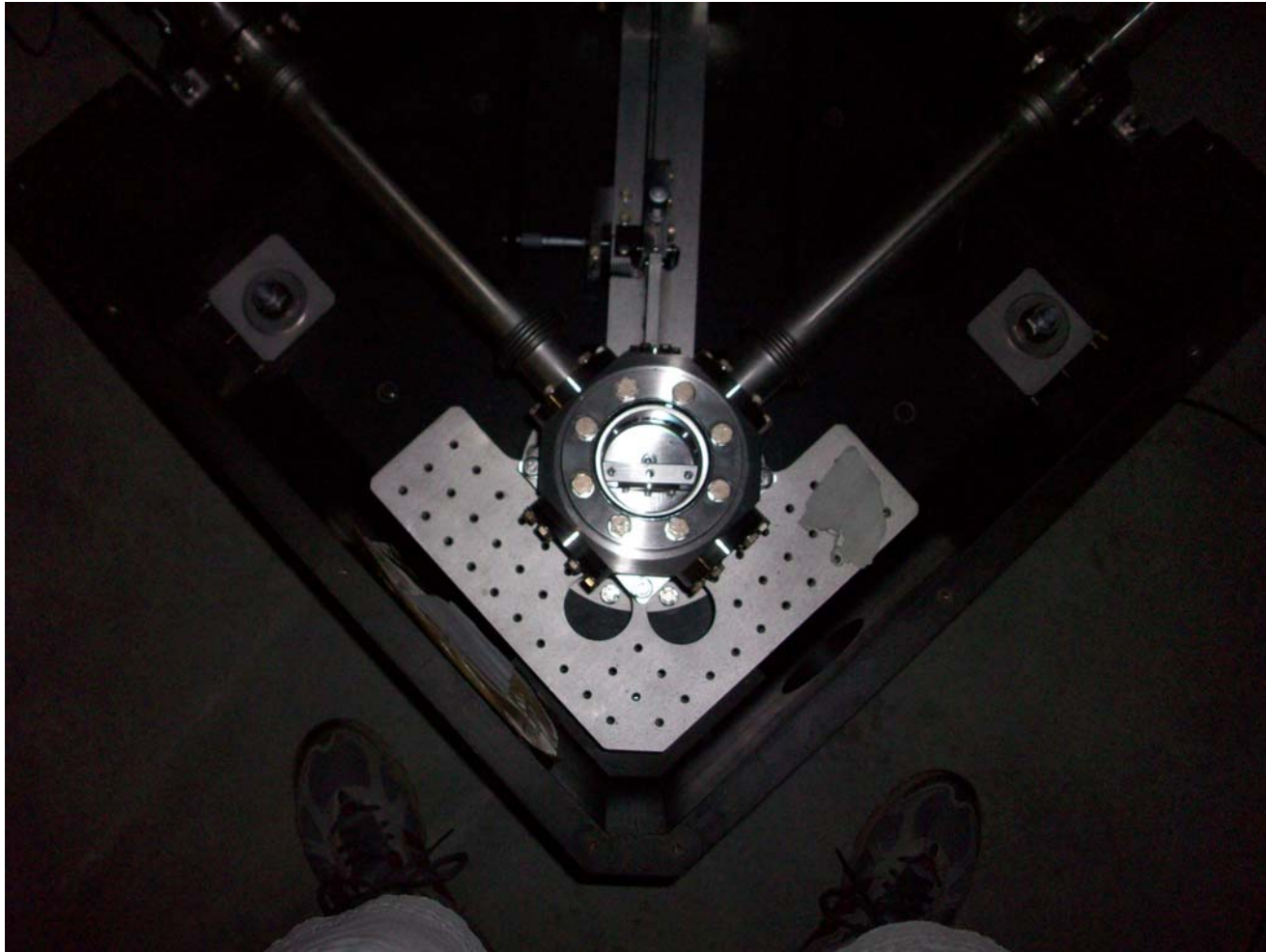




# PFO



# PFO

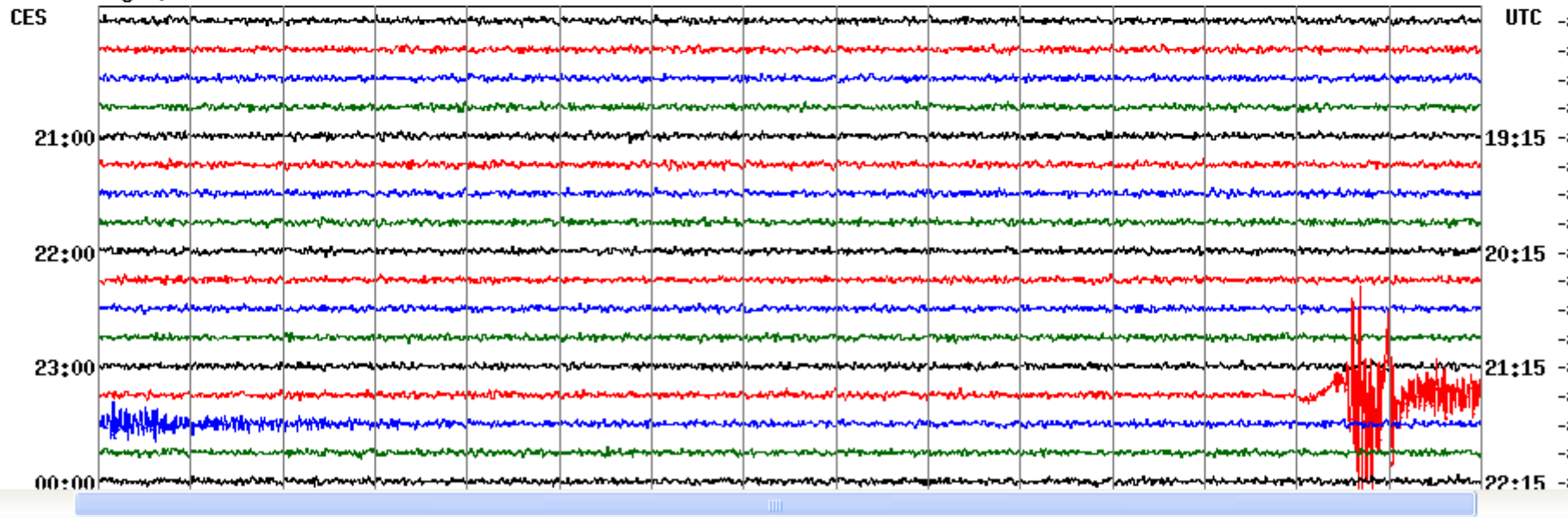




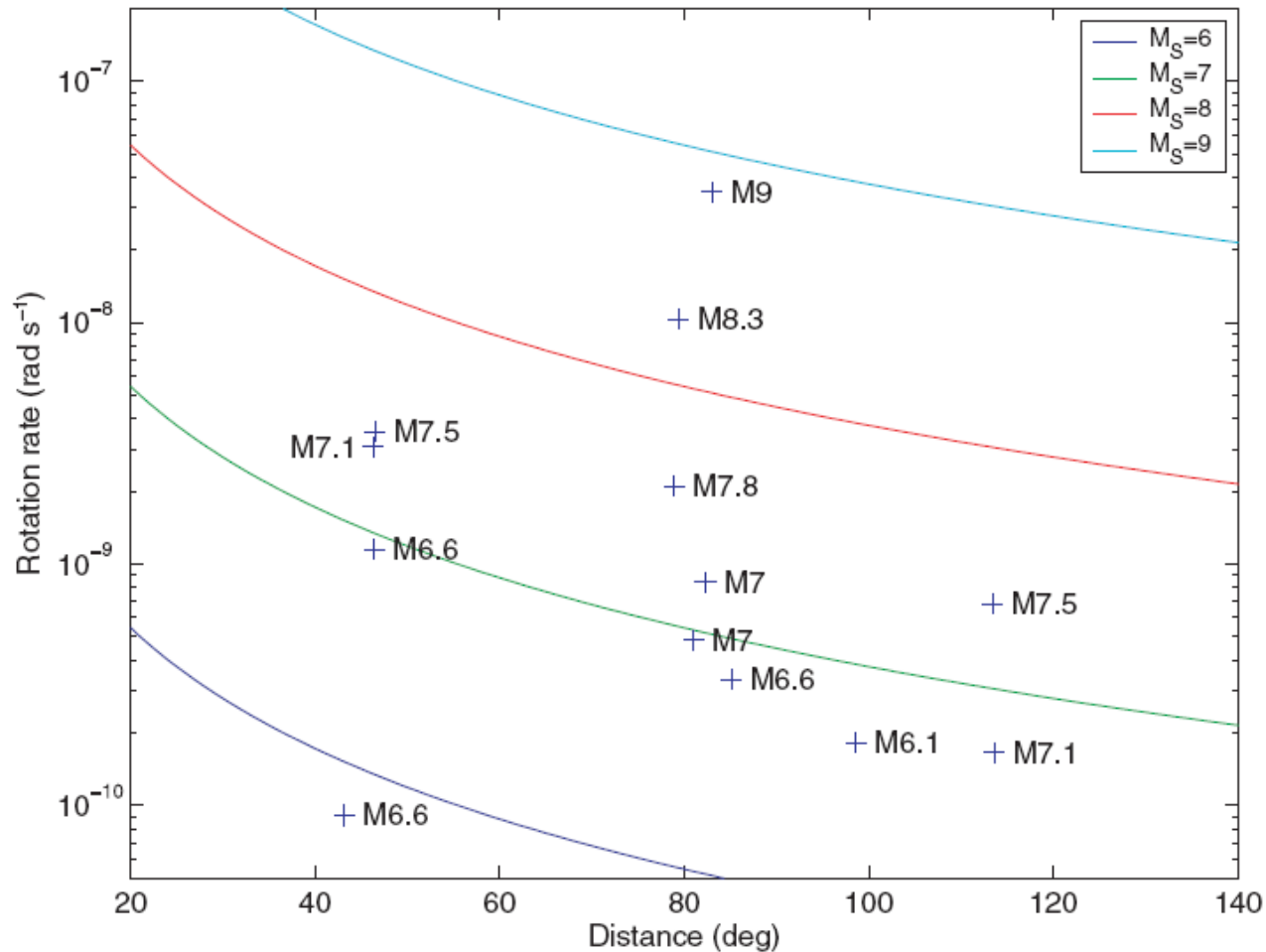
# Data

station: 
 year: 
 month: 
 day: 
 hour:

May 7, 2009 BRLAS BAZ BW 01 (RL-WETZELL-DFM)

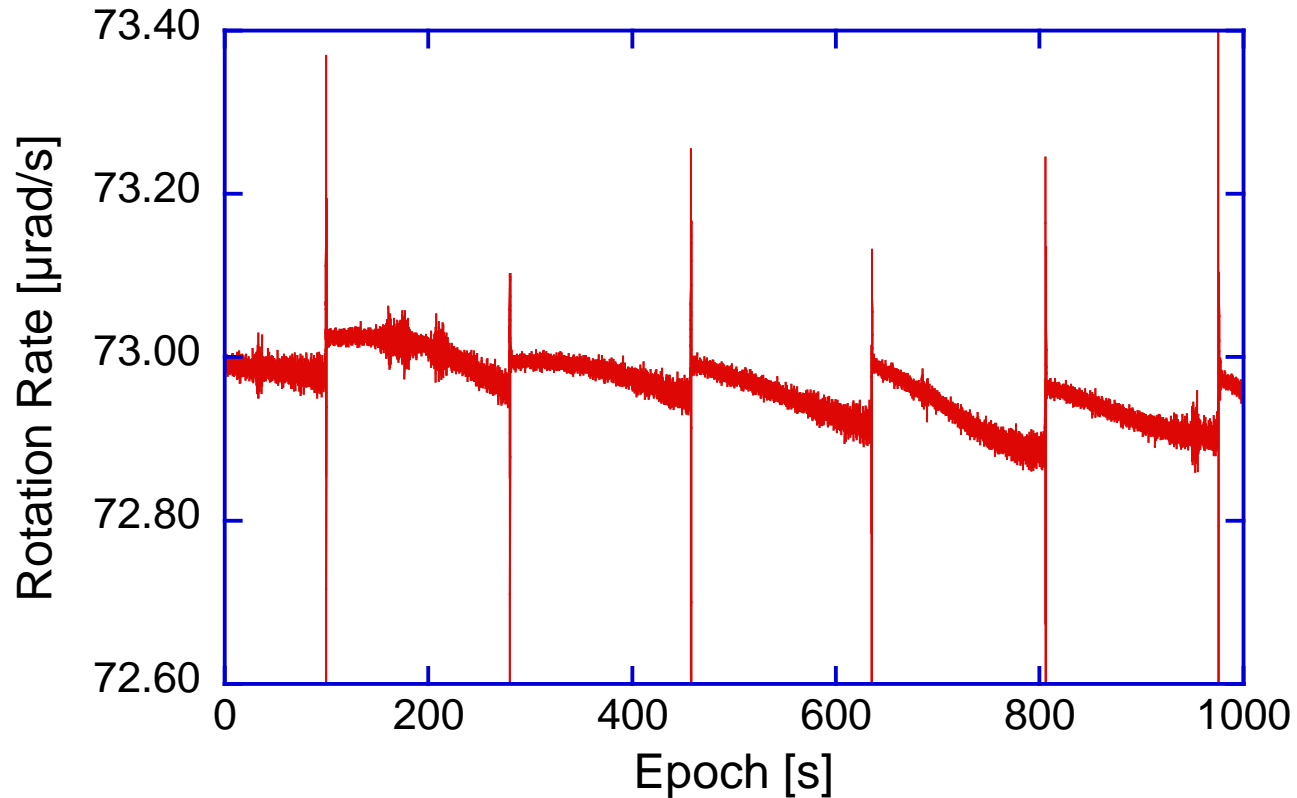


# Expected amplitudes teleseismic events



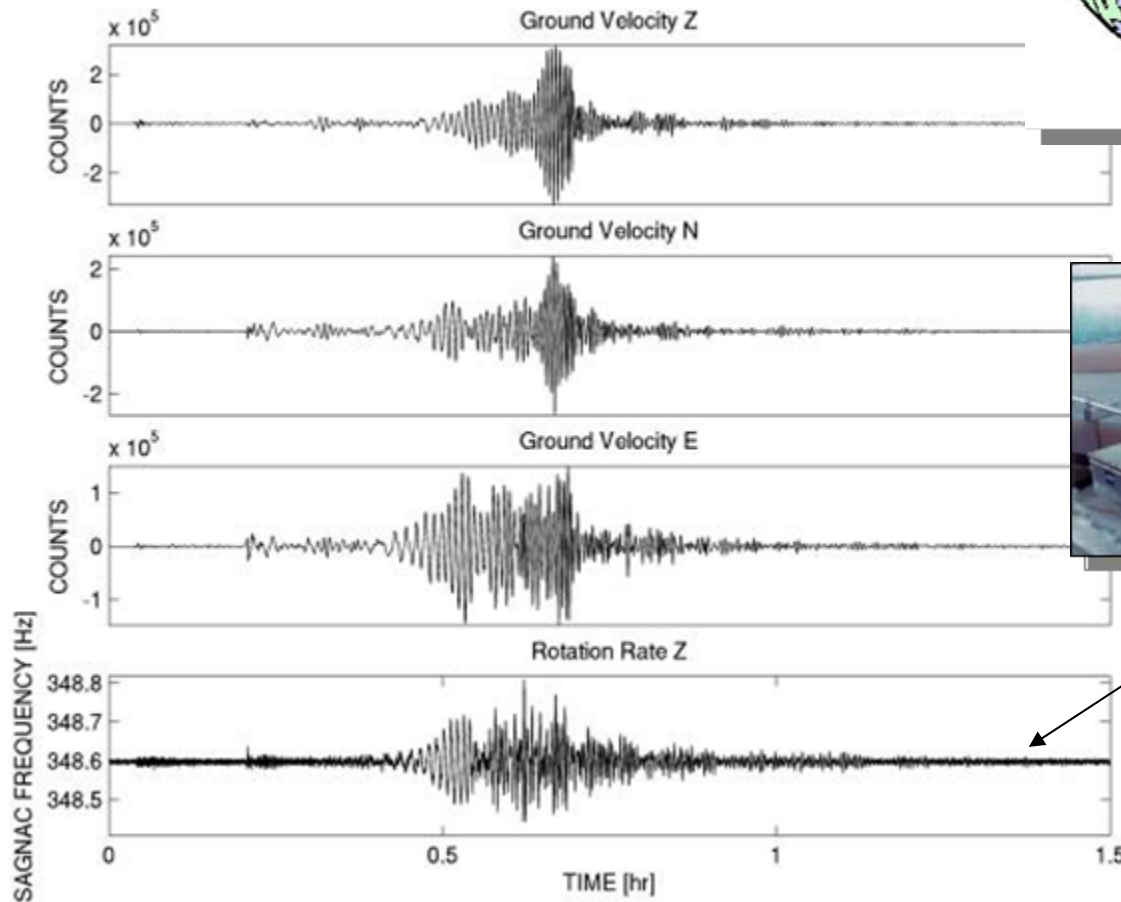
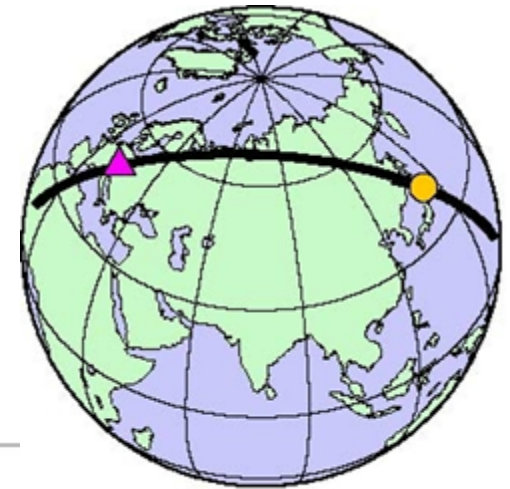
From Igel et al., 2007

# The PFO sensor – mode hops

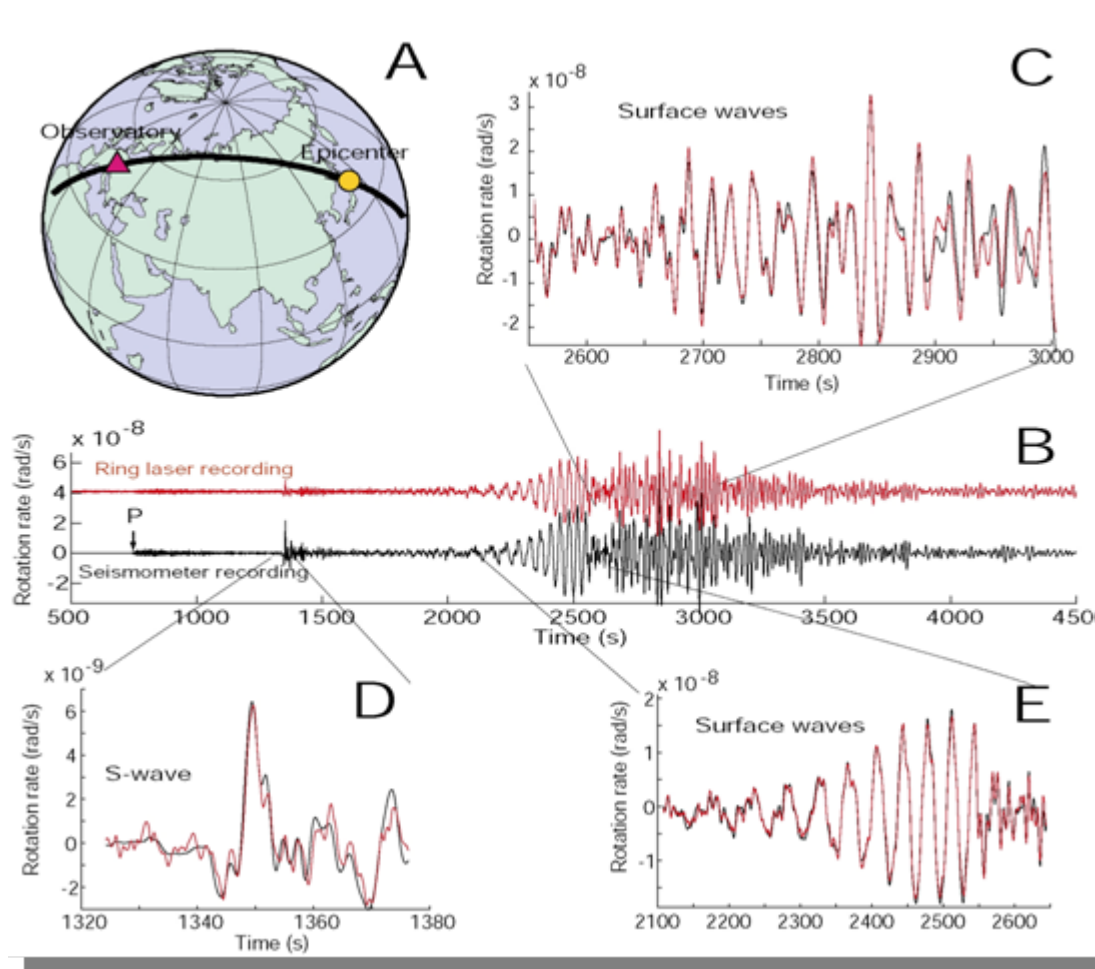


# 4C recordings – raw data

Mw = 8.3 Tokachi-oki earthquake  
25.09.2003 19:50:38.2 GMT  
Lat= 42.21 Lon= 143.84



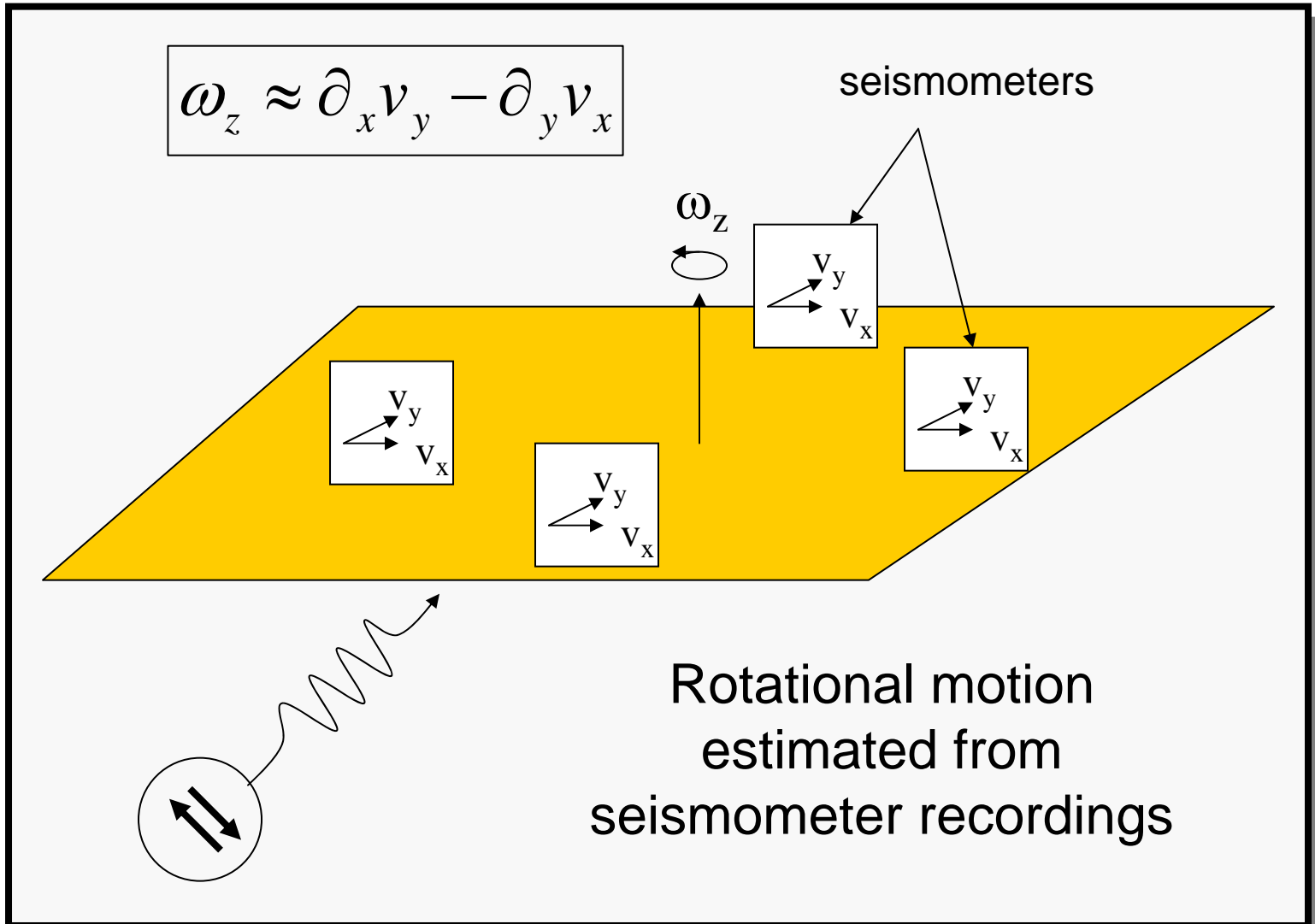
# Mw = 8.3 Tokachi-oki 25.09.2003 transverse acceleration – rotation rate



From Igel et al., GRL, 2005

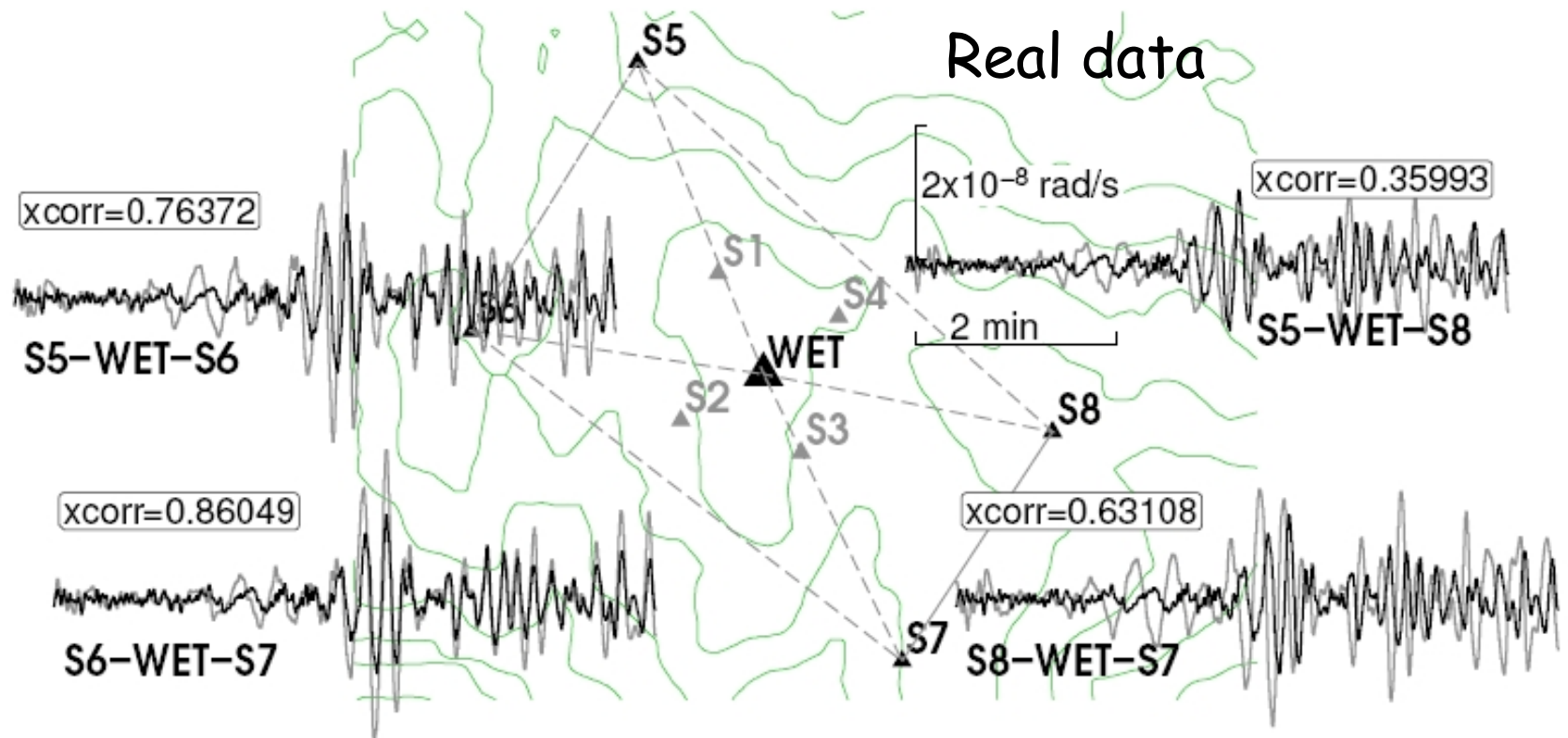
# Rotation from seismic arrays?

... by finite differencing ...

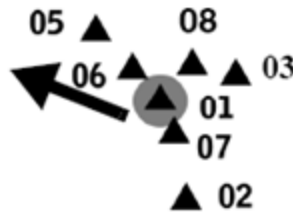
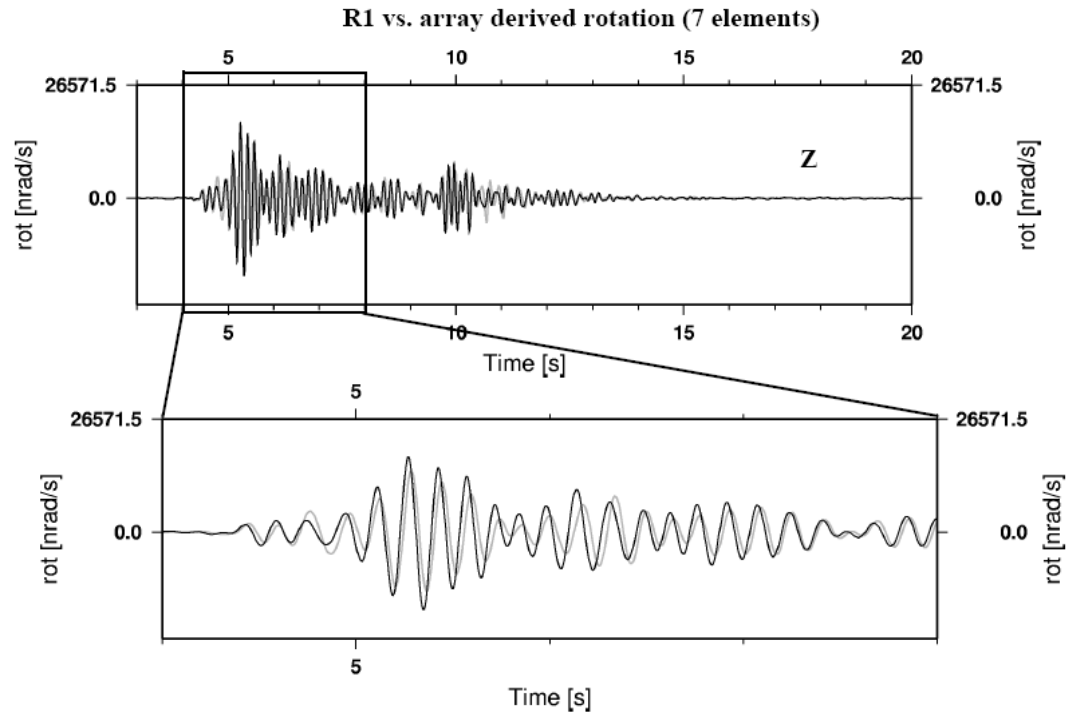




# Uniformity of rotation rate across array



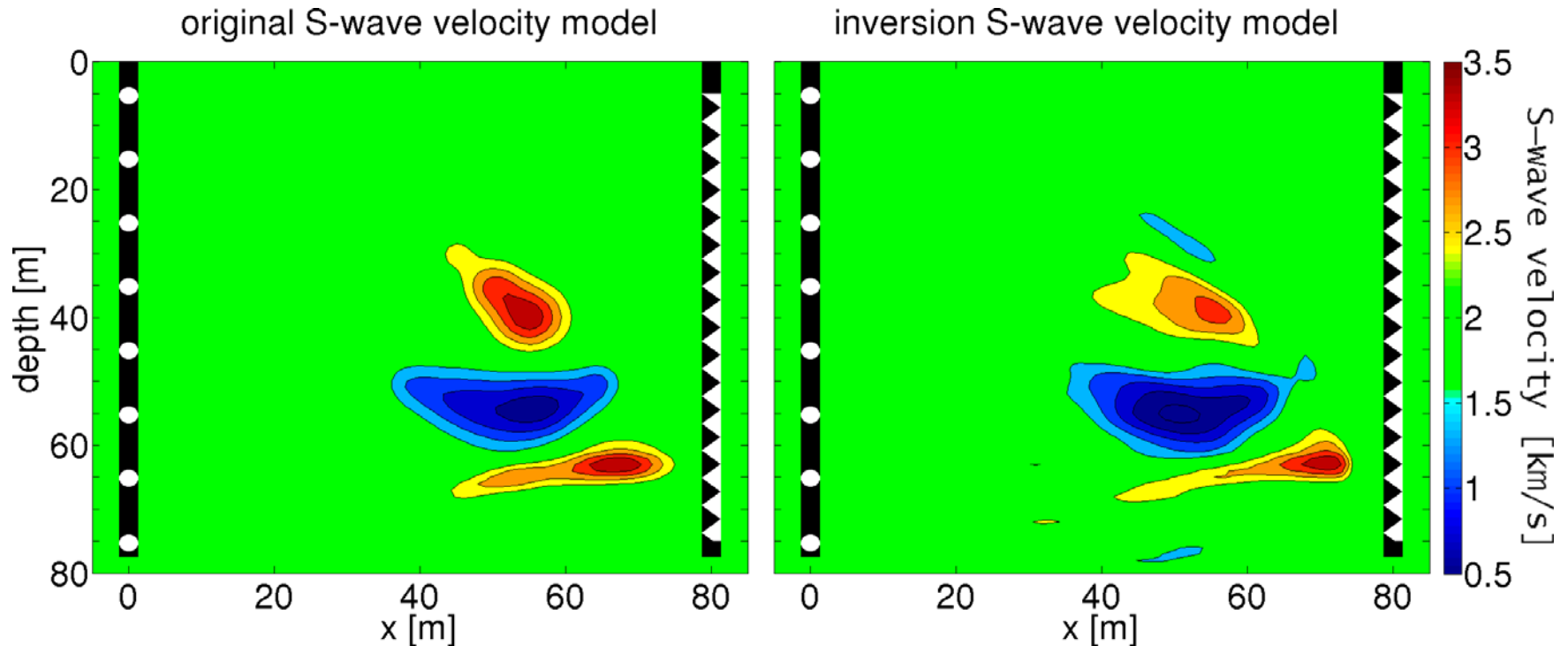
# Array vs. direct measurements



Wassermann et al., 2009, BSSA

# A look to the future

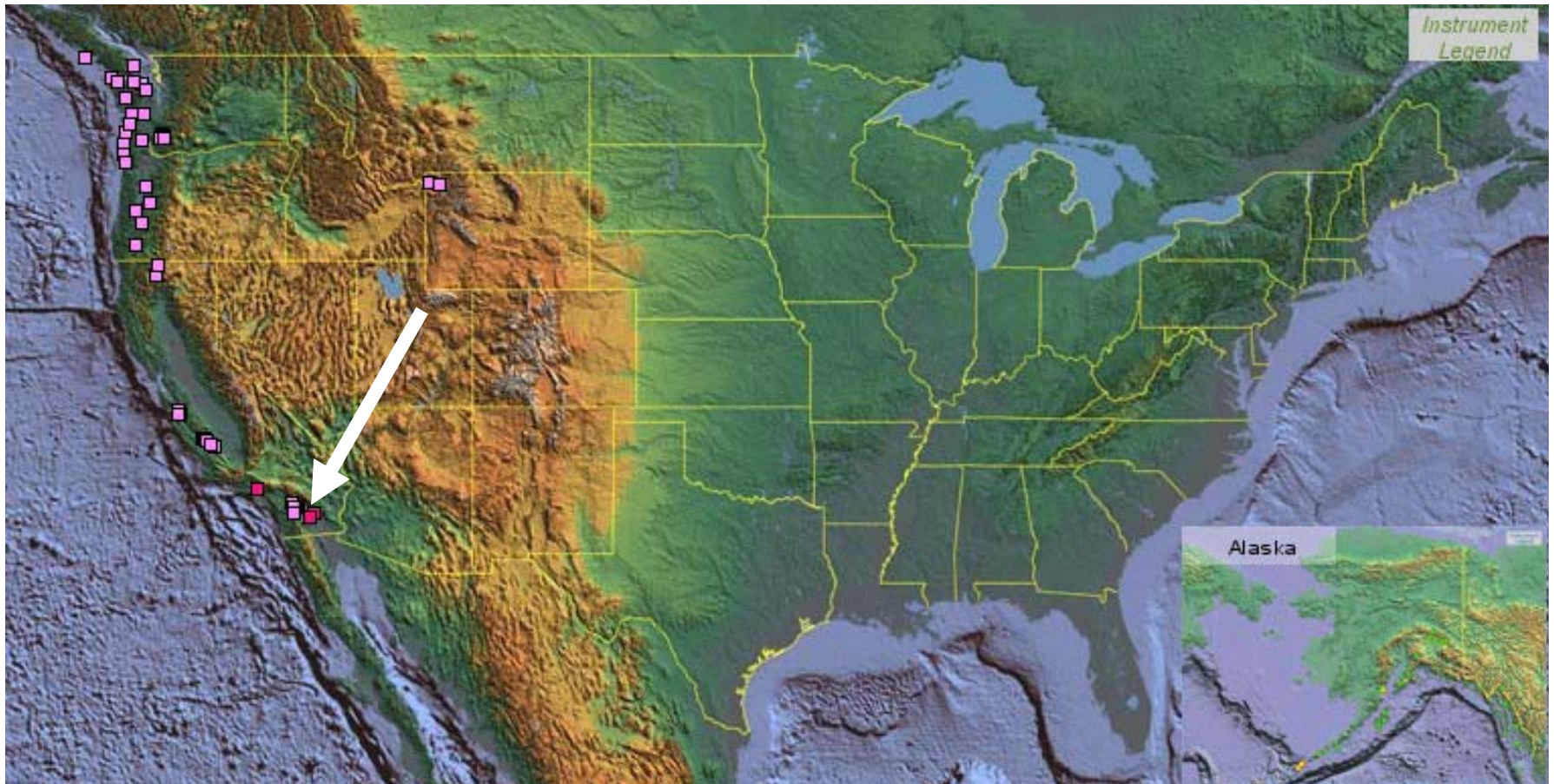
## seismic tomography with rotations



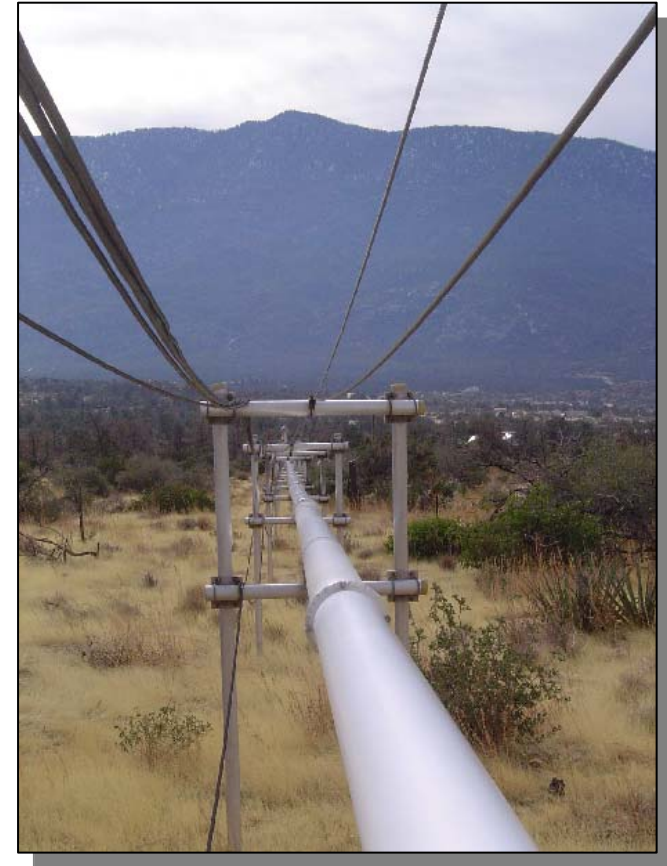
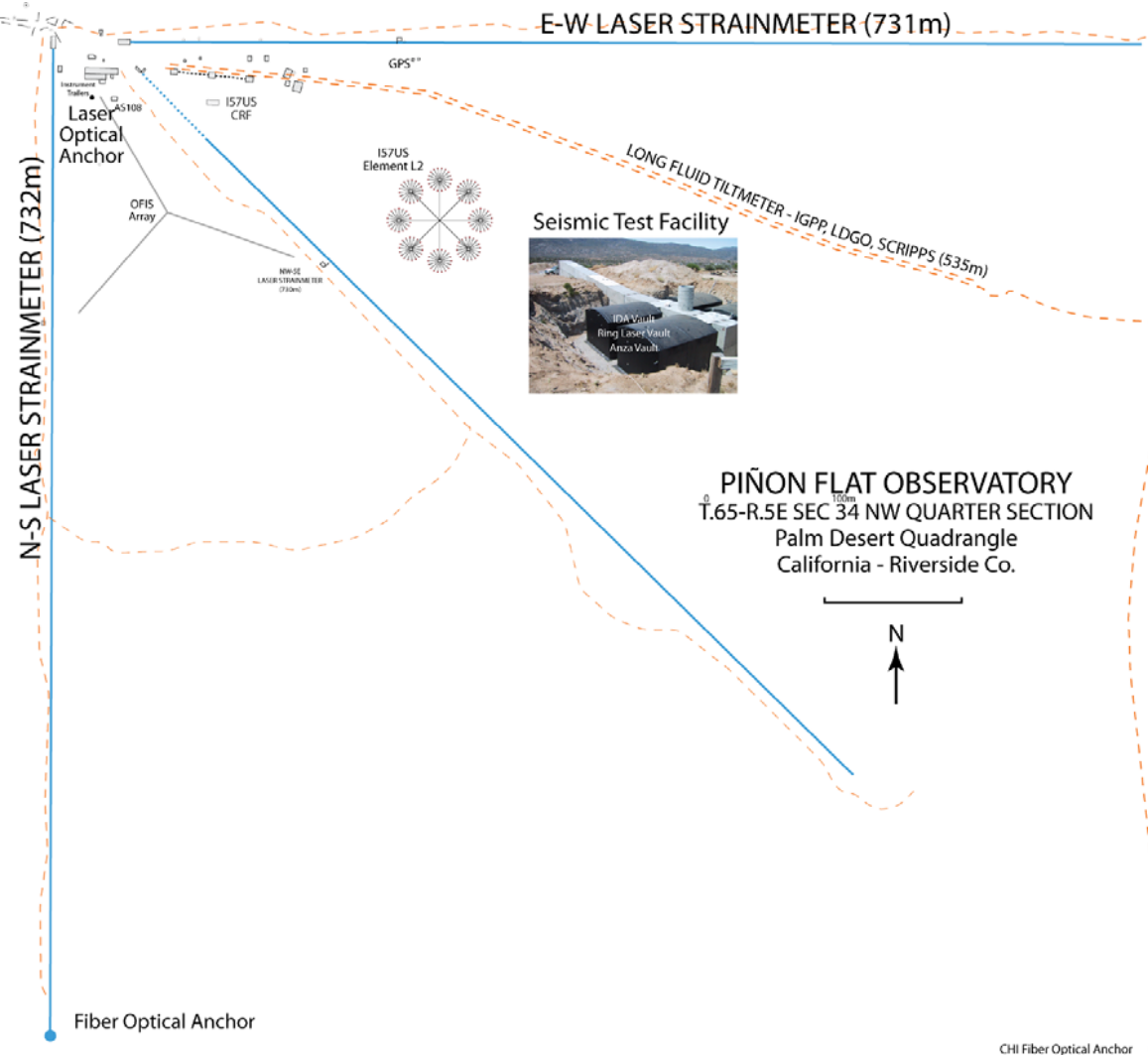
From Bernauer et al., Geophysics, 2009

# Strain sensors

## Network in EarthScope



# Pinon Flat Observatory, CA



# Strain meter principle

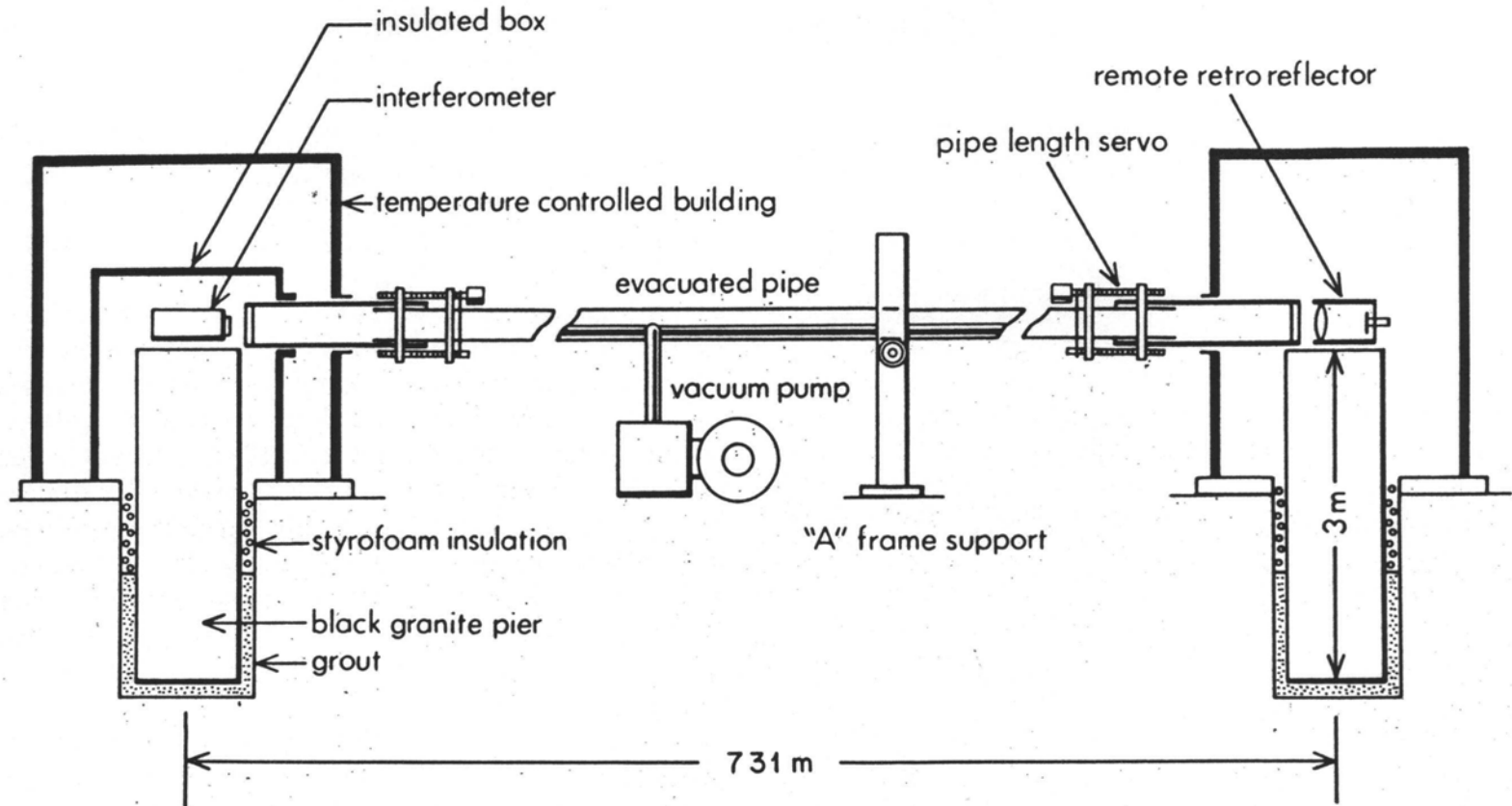
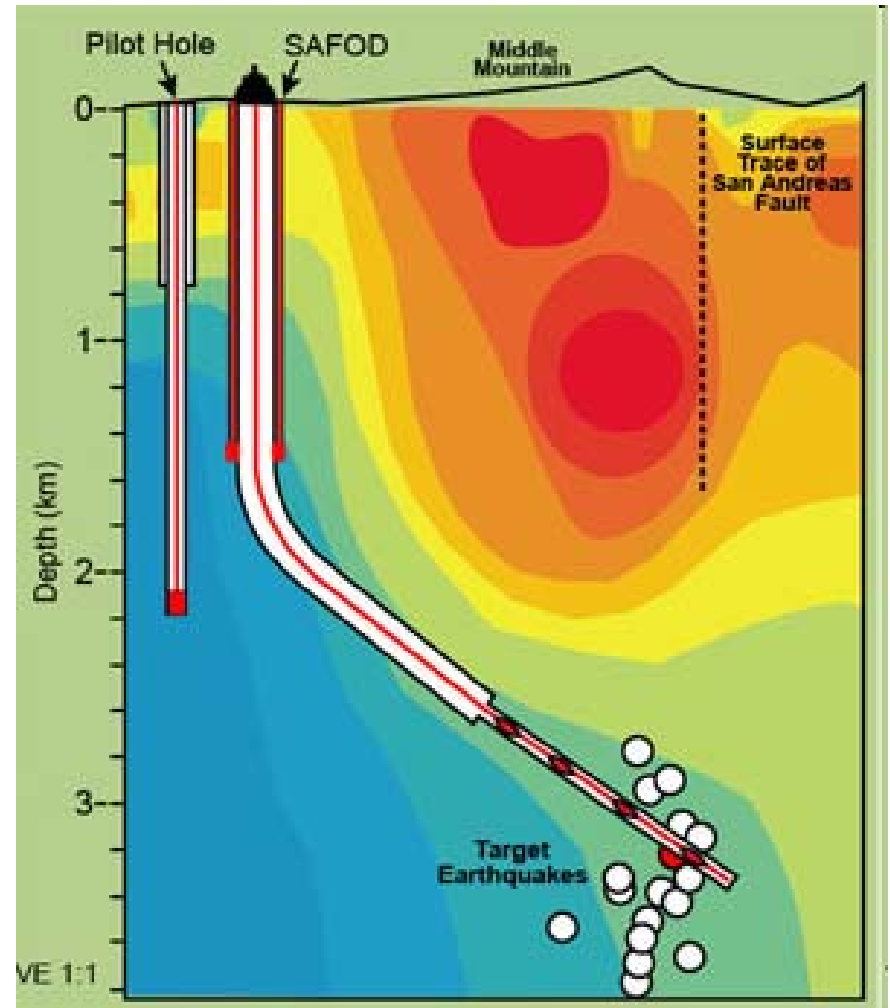
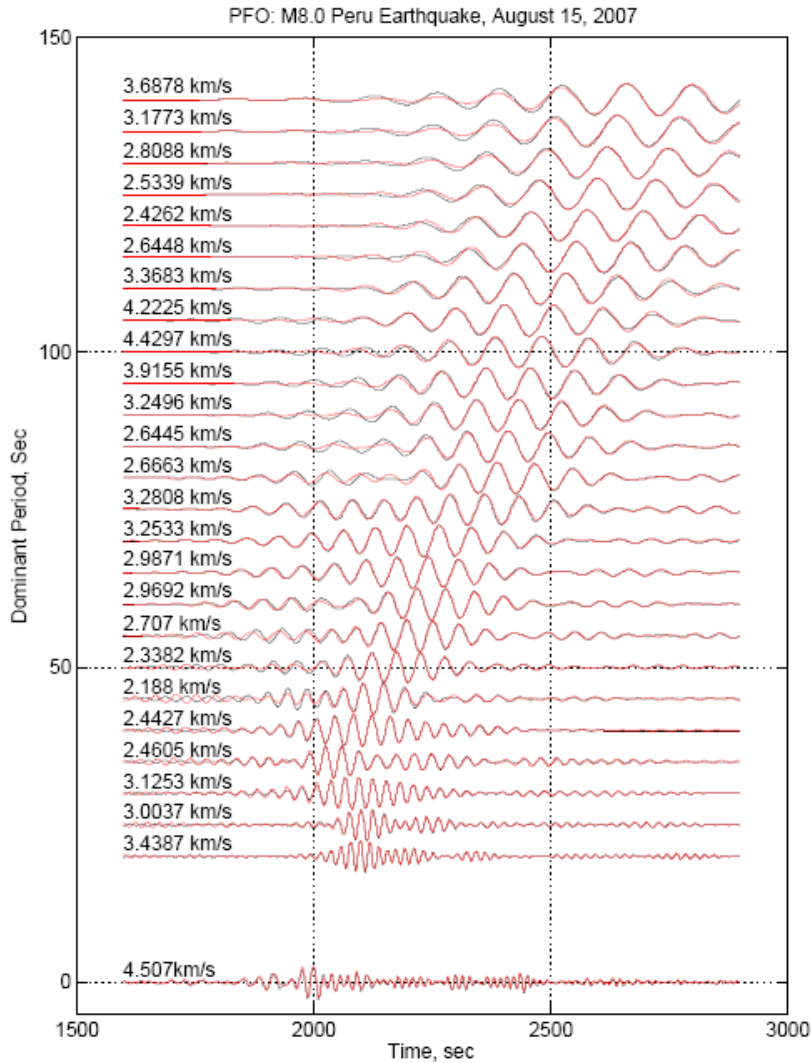


Fig. 21. Mechanical design of the UCSD laser strainmeter. The two endpoints are tall piers of dimension stone sunk in the ground. These, and the optics they carry, are inside temperature-controlled enclosures in air-conditioned buildings. The measurement path is inside a vacuum pipe except at the very ends; telescopic joints keep the length of the air paths constant.

# Interferometer

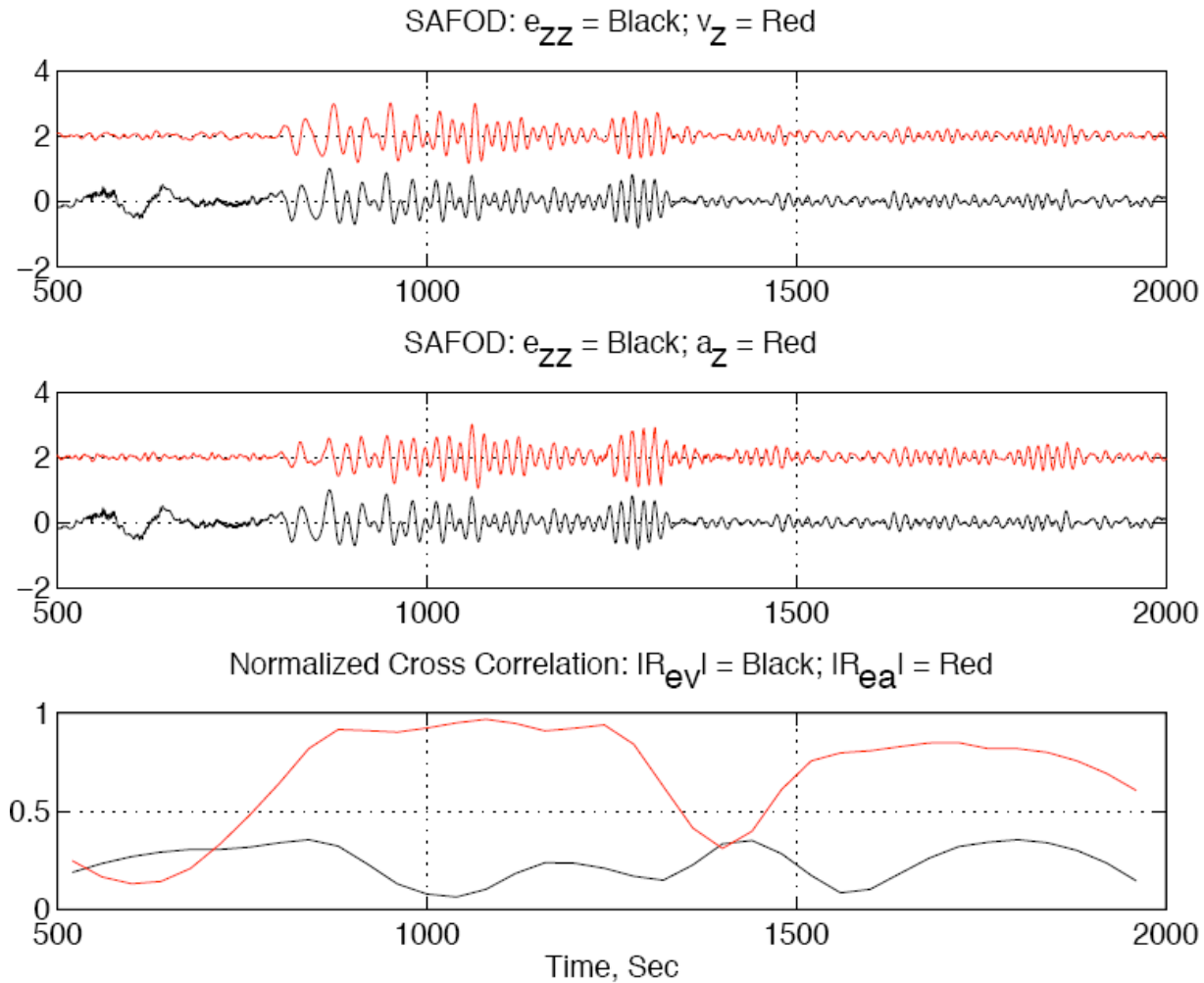


# Strain - Observations



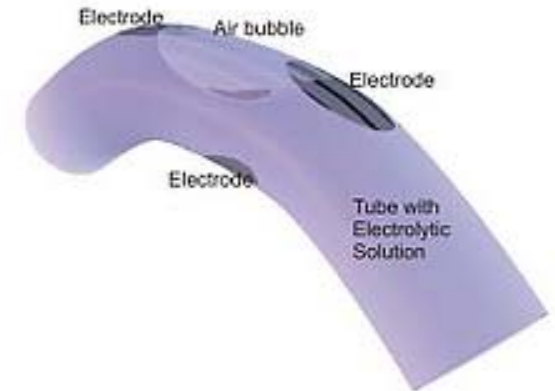


# Strain vs. translations (velocity $v$ , acceleration $a$ )



# Tiltmeters

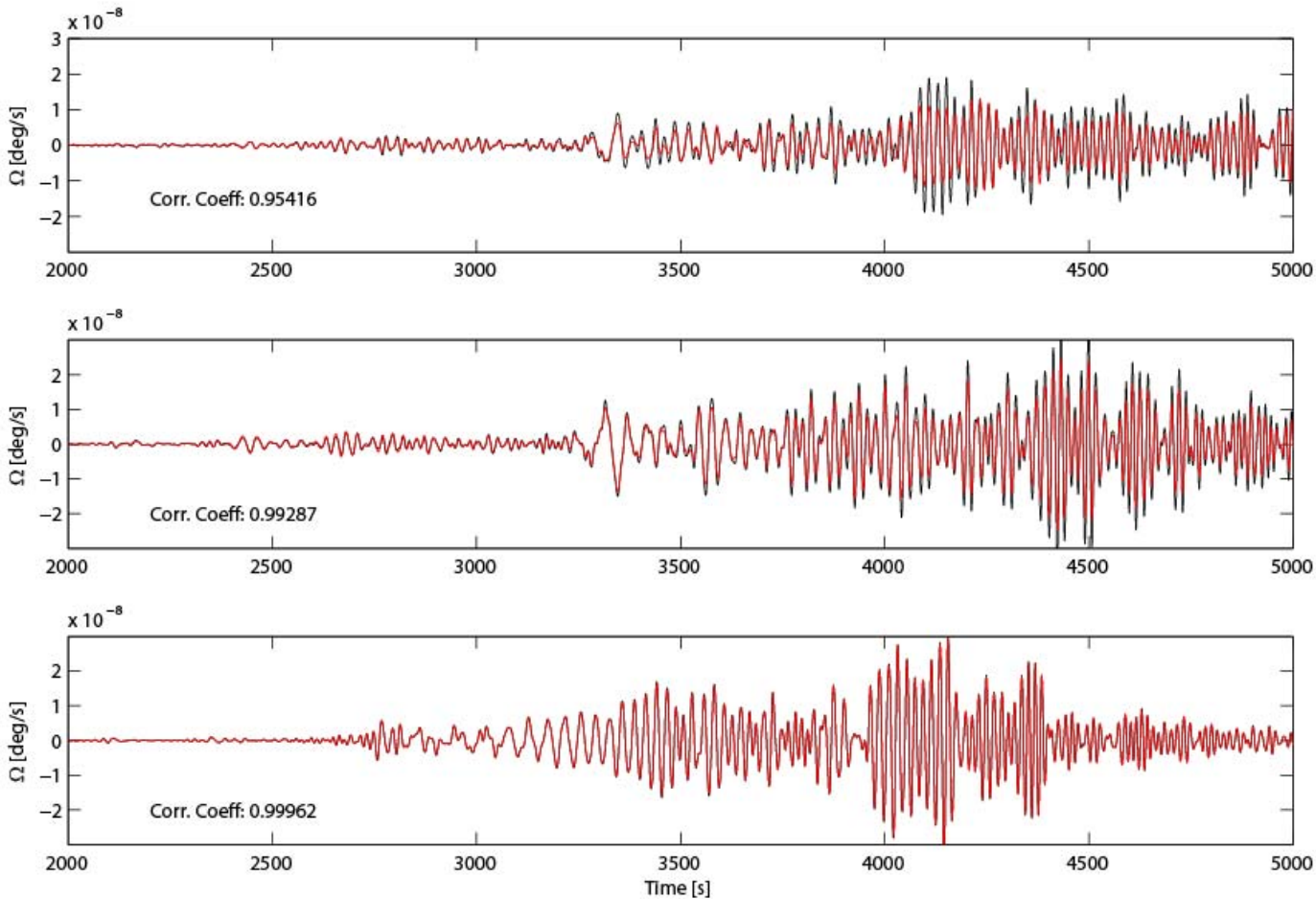
- Tiltmeters are designed to measure changes in the angle of the surface normal
- These changes are particularly important near volcanoes, or in structural engineering
- In the seismic frequency band tiltmeters are sensitive to transverse acceleration



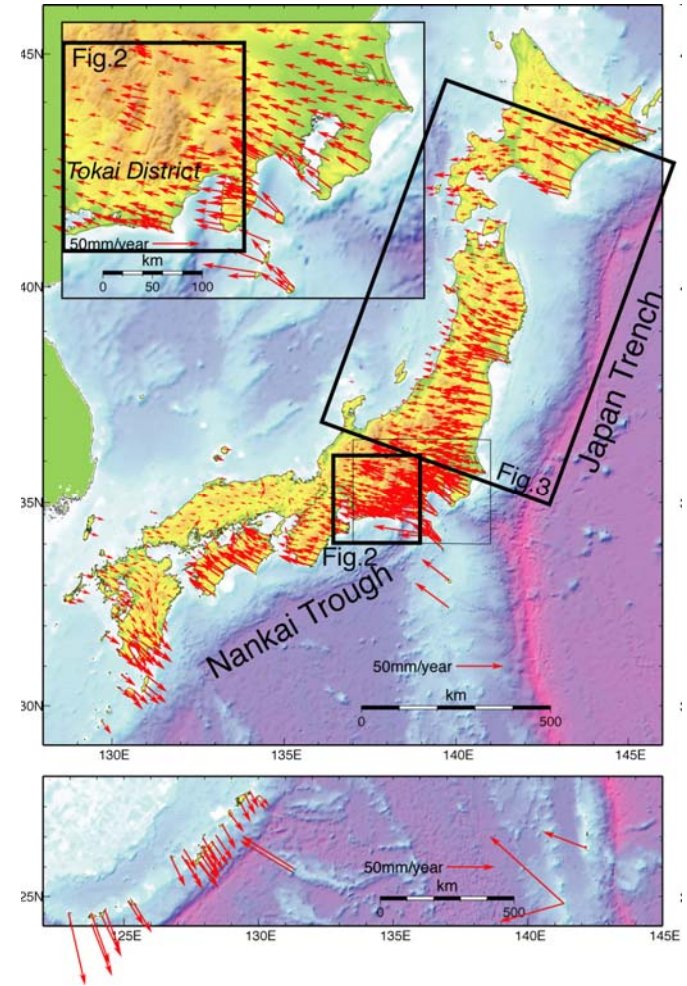
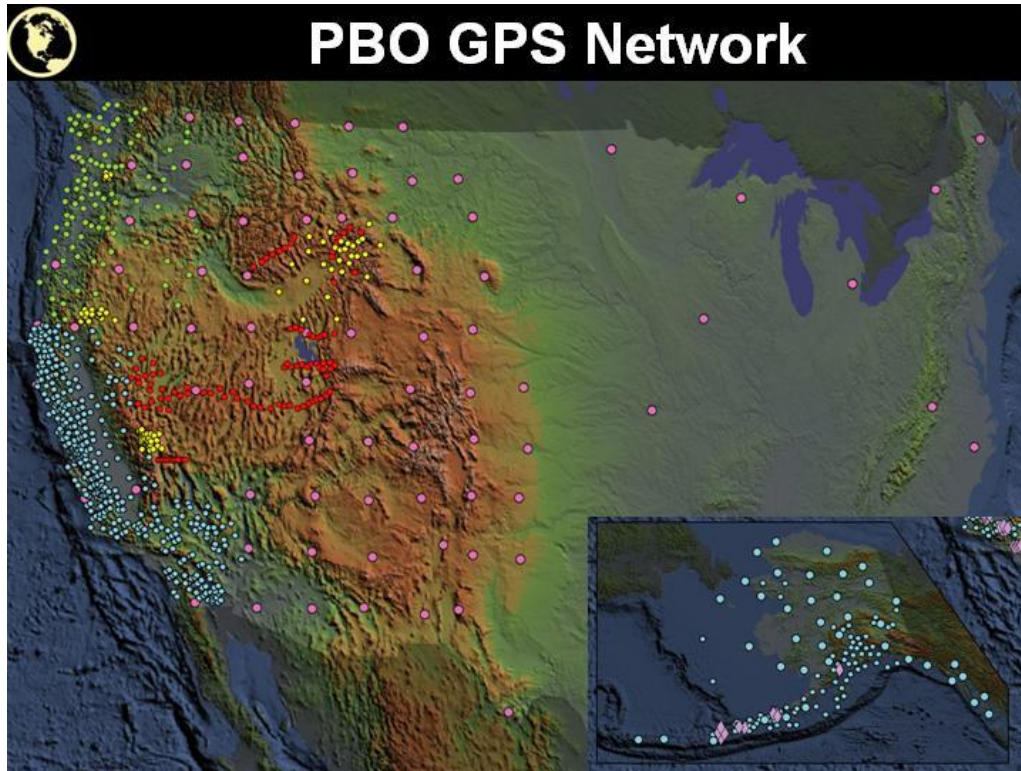
Source: USGS

# Tilt vs. horizontal acceleration

Earthquake recorded at Wettzell, Germany



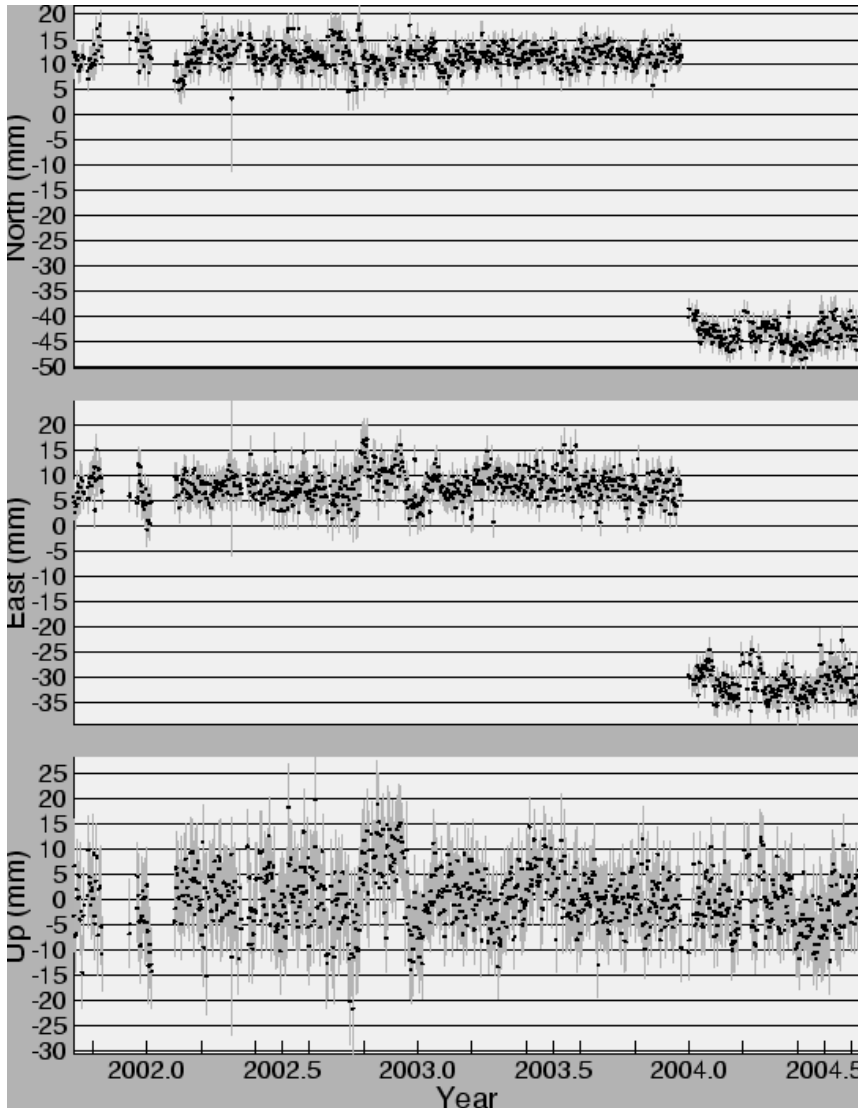
# GPS Sensor Networks



# San Francisco GPS Network

Co-seismic displacement measured in California during an earthquake.

(Source: UC Berkeley)



# Other sensors and curiosities

- Gravimeters
- Ground water level
- Electromagnetic measurements (ionosphere)
- Infrasound measurements

# Summary

- Seismometers are forced oscillators, recorded seismograms have to be corrected for the instrument response
- Strains and rotations are usually measured with optical interferometry, the accuracy is lower than for standard seismometers
- The goal in seismology is to measure with one instrument a broad frequency and amplitude range (broadband instruments)
- Cross-axis sensitivity is an important current issue (translation – rotation – tilt)